

Towards a complete description of the neutrinoless double beta decay

Mihai Horoi

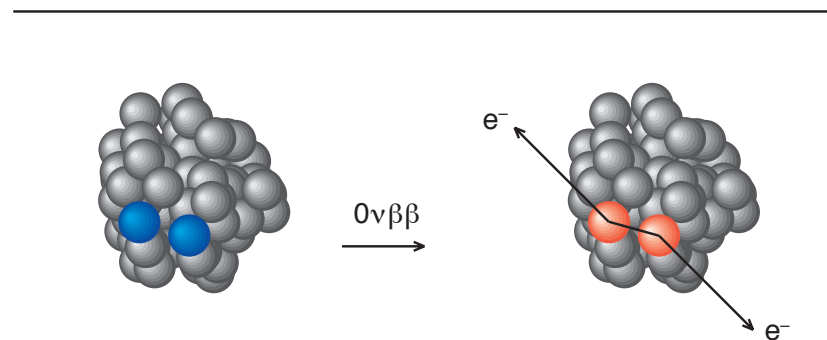
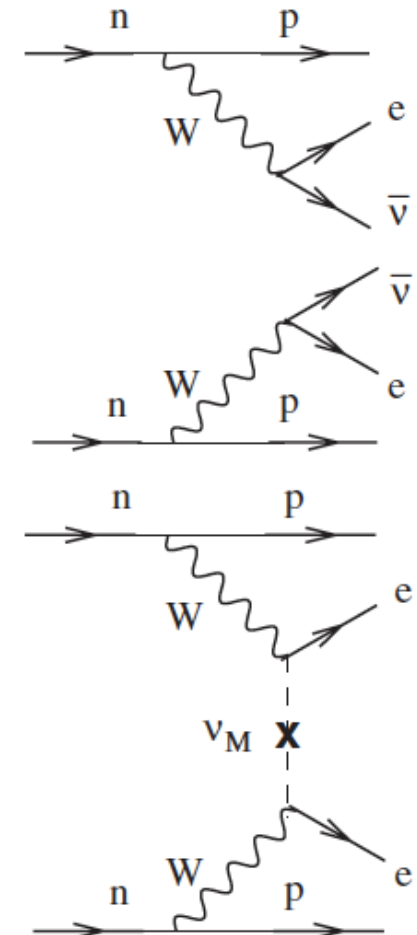
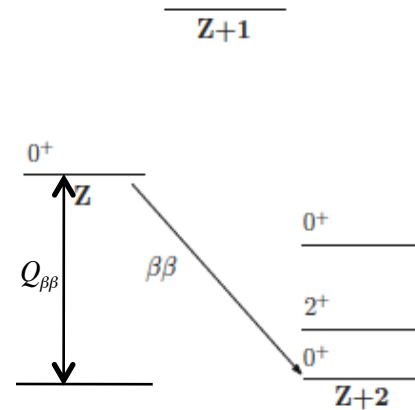
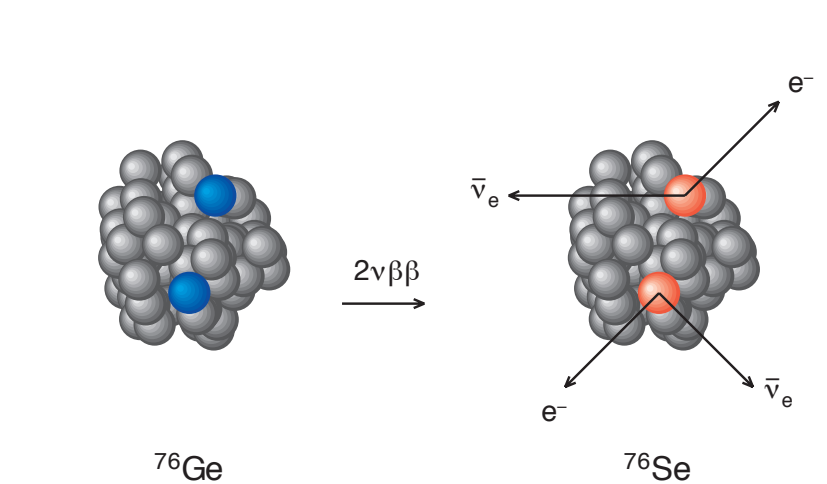
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➤ Support from NSF grant PHY-1404442, DOE grants DE-SC0008529, and DE-SC0015376 is acknowledged

MEDEX17, May 29,
2017

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Classical Double Beta Decay Problem



$$\langle m_{\beta\beta} \rangle = \left| \sum_k m_k U_{ek}^2 \right|$$

$$T_{1/2}^{-1}(0\nu) = G^{0\nu} (Q_{\beta\beta}) \left[M^{0\nu}(0^+) \right]^2 \left(\frac{\langle m_{\beta\beta} \rangle}{m_e} \right)^2$$

The Nobel Prize in Physics 2015



Photo © Takaaki Kajita

Takaaki Kajita

Prize share: 1/2



Photo: K. McFarlane.
Queen's University
/SNOLAB

Arthur B. McDonald

Prize share: 1/2

The Nobel Prize in Physics 2015 was awarded jointly to Takaaki Kajita and Arthur B. McDonald *"for the discovery of neutrino oscillations, which shows that neutrinos have mass"*

$$|\nu_\alpha\rangle = \sum U_{\alpha i}^* |\nu_i\rangle$$

$$|\nu_i\rangle = \sum_\alpha U_{\alpha i} |\nu_\alpha\rangle$$

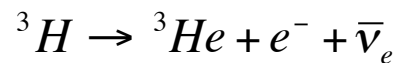
Neutrino Masses

PMNS – matrix

$$U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix} \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$c_{12} \equiv \cos\theta_{12}, \quad s_{12} = \sin\theta_{12}, \text{ etc}$$

- Tritium decay:



$$m_{\nu_e} = \sqrt{\sum_i |U_{ei}|^2 m_i^2} < 2.2 \text{ eV (Mainz exp.)}$$

KATRIN (to take data): goal $m_{\nu_e} < 0.3 \text{ eV}$

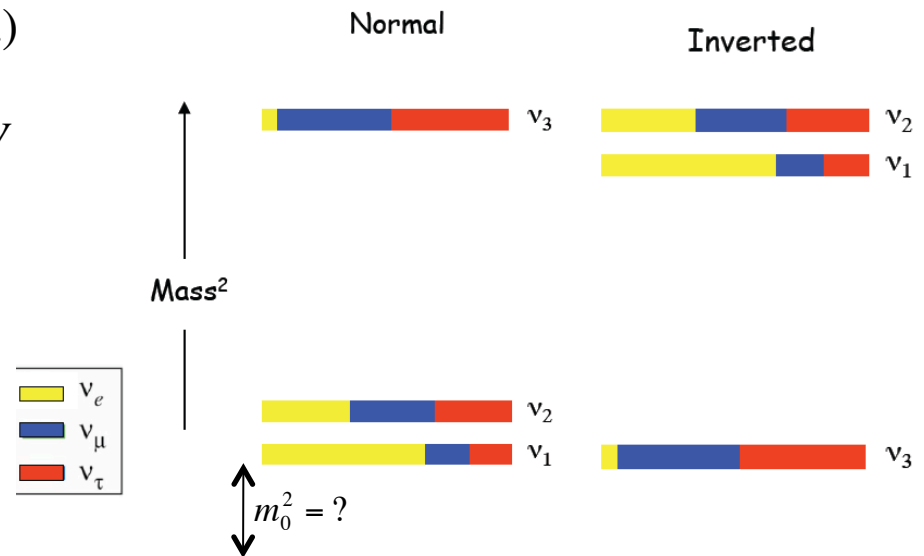
- Cosmology: CMB power spectrum, BAO, etc,

$$\sum_{i=1}^3 m_i < 0.23 \text{ eV}$$

Goal: 0.01 eV (5 – 10 y)

$$\Delta m_{21}^2 \approx 7.5 \times 10^{-5} \text{ eV}^2 (\text{solar})$$

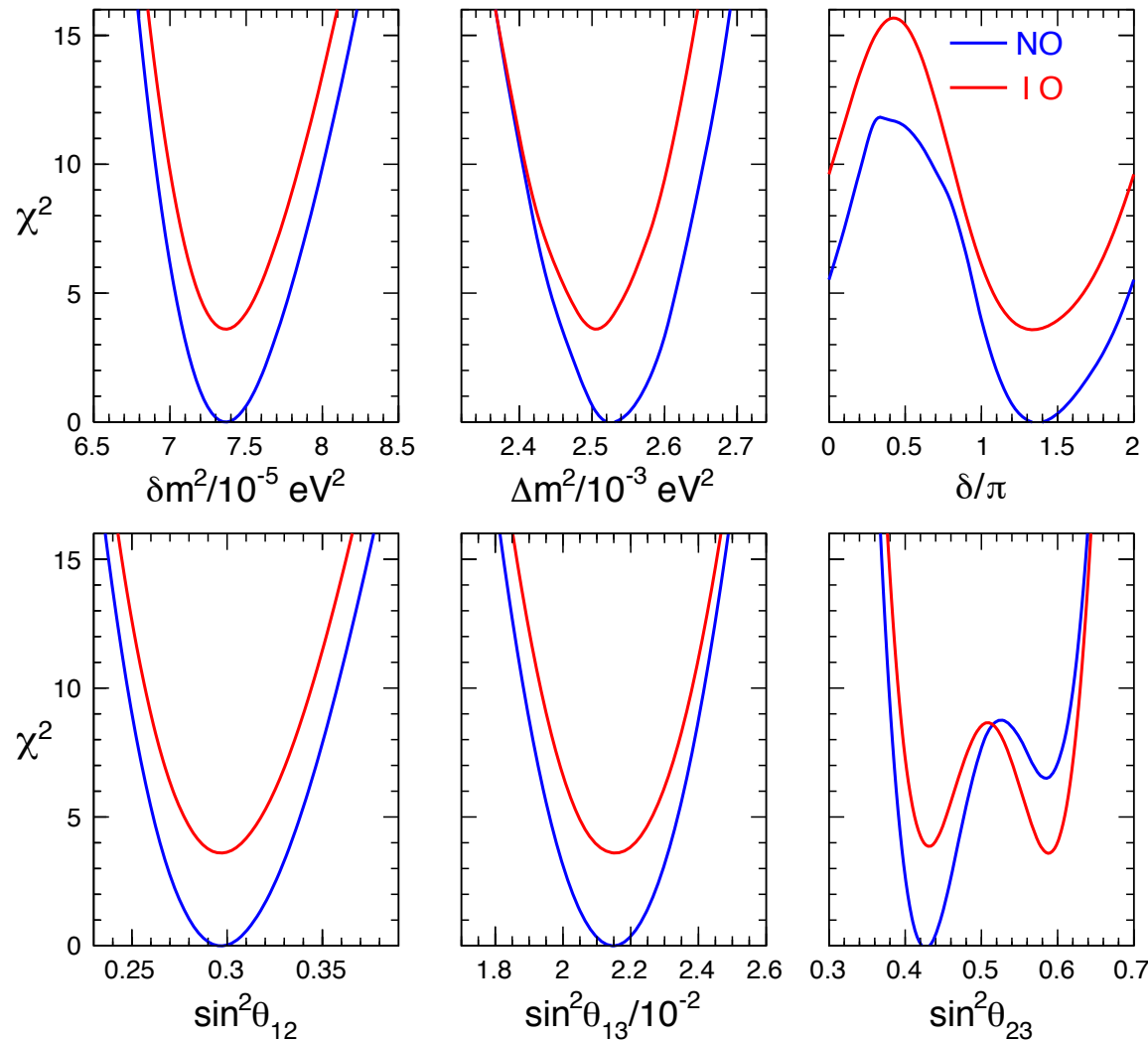
$$|\Delta m_{32}^2| \approx 2.4 \times 10^{-3} \text{ eV}^2 (\text{atmospheric})$$



Two neutrino mass hierarchies

Neutrino oscillations parameters

Oscillation parameters



Bari group:

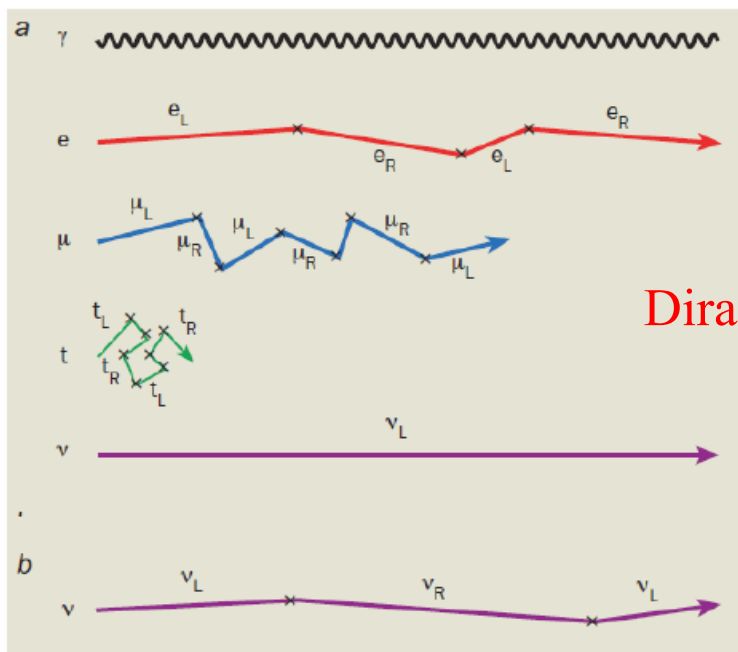
arxiv.org/1703.04471

$$(\Delta\chi^2_{\text{IO-NO}})^{1/2} = 2$$

Neutrino masses: Dirac vs Majorana

The fermions and the W/Z bosons get mass: by interacting with the Higgs field.

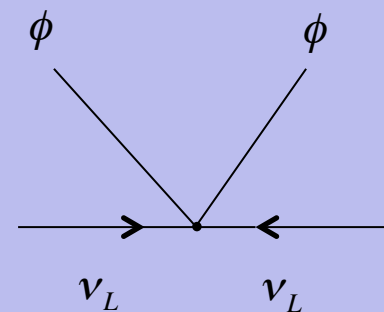
This mechanisms could also work for neutrinos, if they would be Dirac fermions. Then, it would be difficult to explain why their masses (Yukawa couplings) are so small.



The mass terms come from the Yukawa interaction :

$$\bar{\psi}_i Y_{ij} \psi_j \langle \phi \rangle \quad \text{where } \langle \phi \rangle = 246 \text{ GeV}$$

Weinberg's dimension-5
BSM operator contributing
to Majorana neutrino mass



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Fork on the Road: Are Neutrinos Majorana or Dirac Fermions?



Best (Only?) Bet: Neutrinoless Double-Beta Decay.

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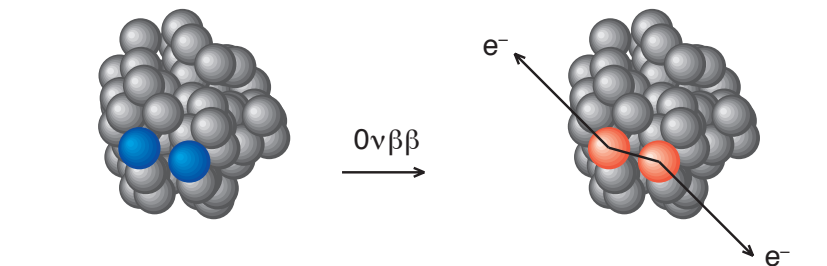
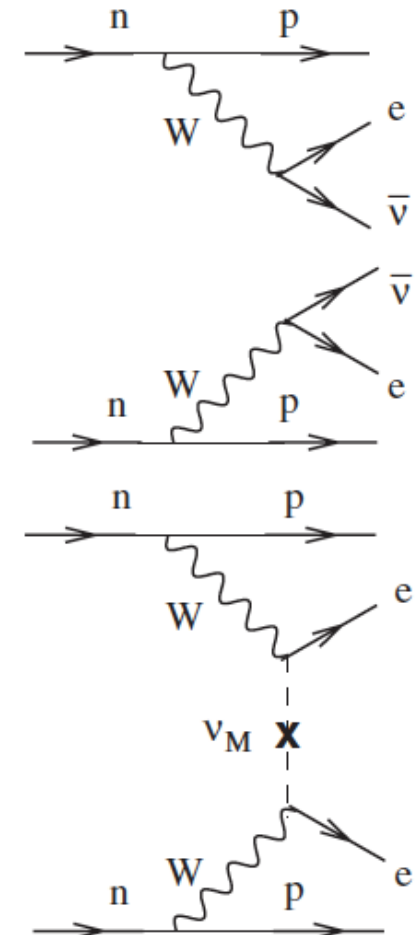
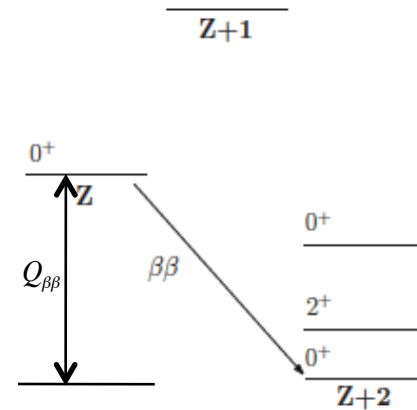
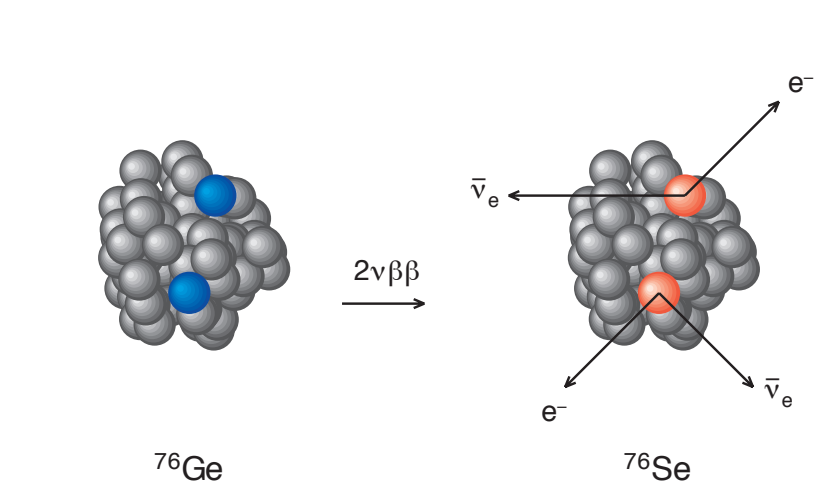
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We learned that neutrinos have mass, but we don't know how to extend the Standard Model!

Nobel prize 2025: Neutrinoless Double Beta Decay?

Probably the best chance of the low-energy nuclear physics community to get another Nobel prize!

Classical Double Beta Decay Problem

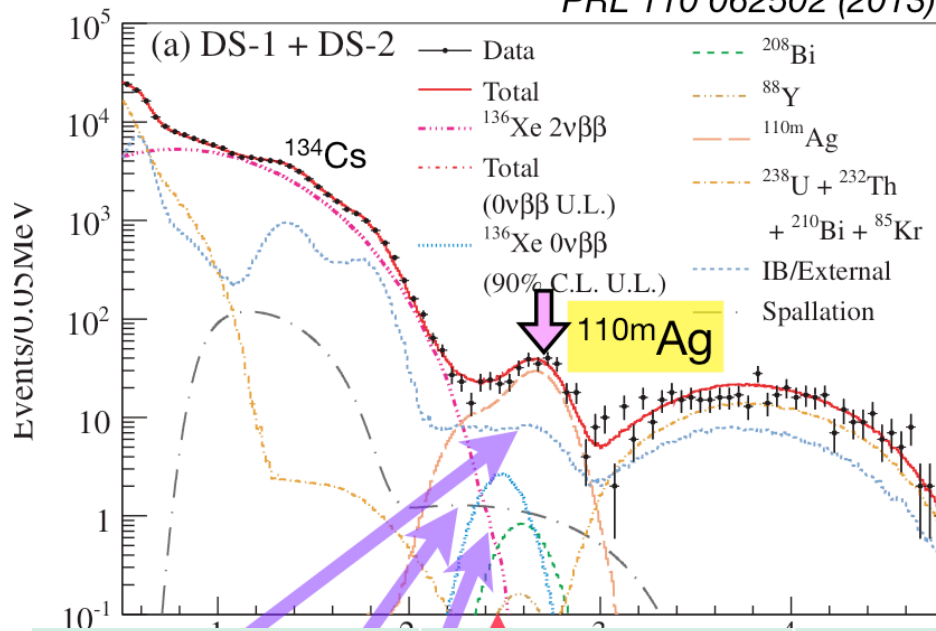


$$\langle m_{\beta\beta} \rangle = \left| \sum_k m_k U_{ek}^2 \right|$$

$$T_{1/2}^{-1}(0\nu) = G^{0\nu} (Q_{\beta\beta}) \left[M^{0\nu}(0^+) \right]^2 \left(\frac{\langle m_{\beta\beta} \rangle}{m_e} \right)^2$$

Phase1 (before purification)

PRL 110 062502 (2013)



¹³⁶Xe ββ Experimental Results

	$T_{1/2}^{0\nu}(\text{lim})$	$T_{1/2}^{0\nu}(\text{Sens})$
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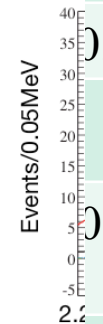
KamLAND-Zen

Half-life limit (@90%C.L.)

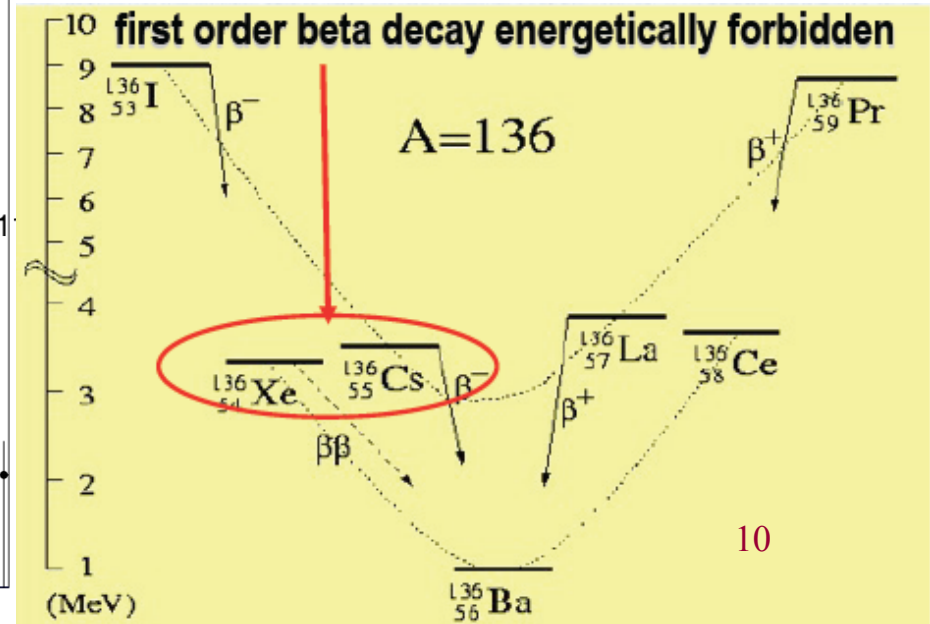
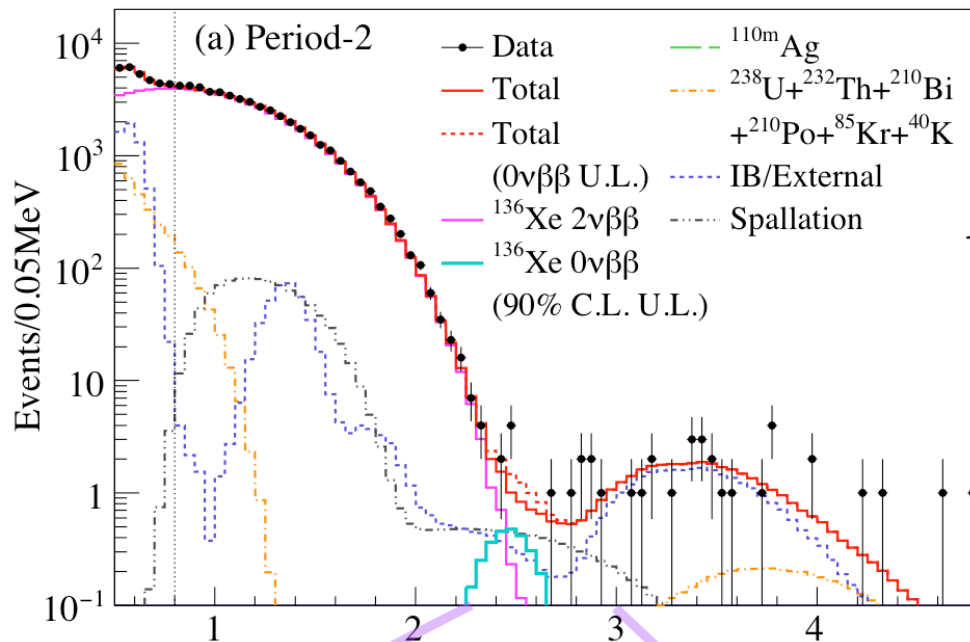
Phase1 $T_{1/2}^{0\nu} > 1.9 \times 10^{25} \text{ yr}$

Phase2 $T_{1/2}^{0\nu} > 9.2 \times 10^{25} \text{ yr}$ **x6!**

Combined $T_{1/2}^{0\nu} > 1.07 \times 10^{26} \text{ yr}$



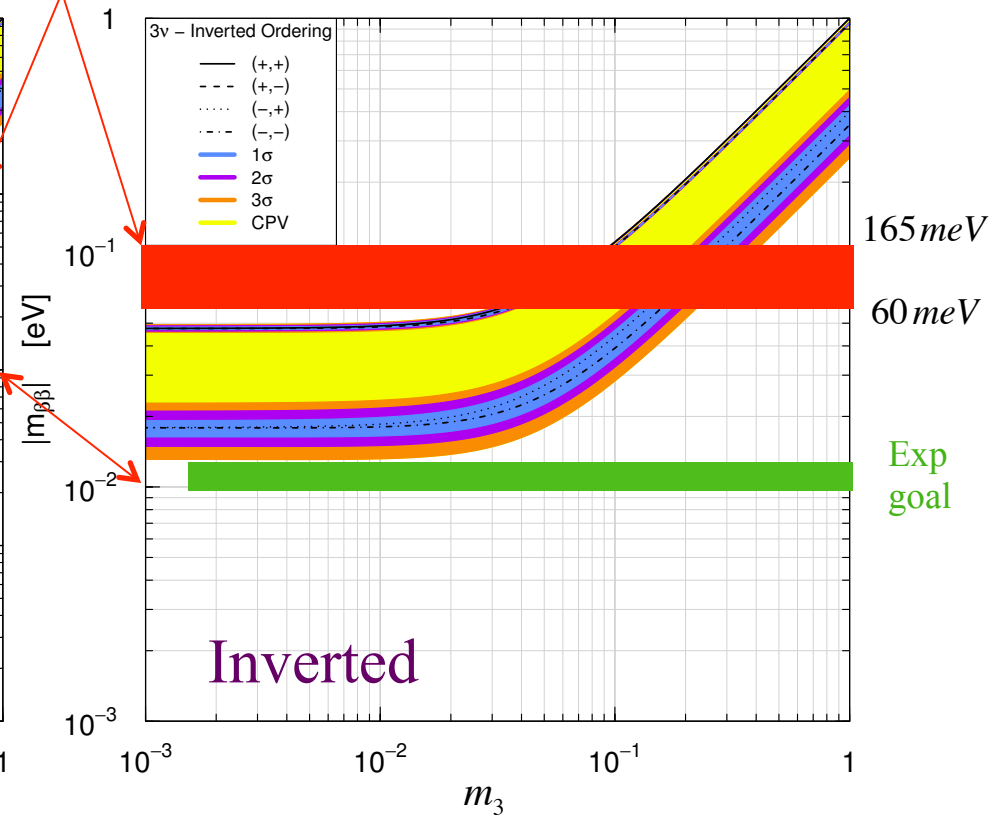
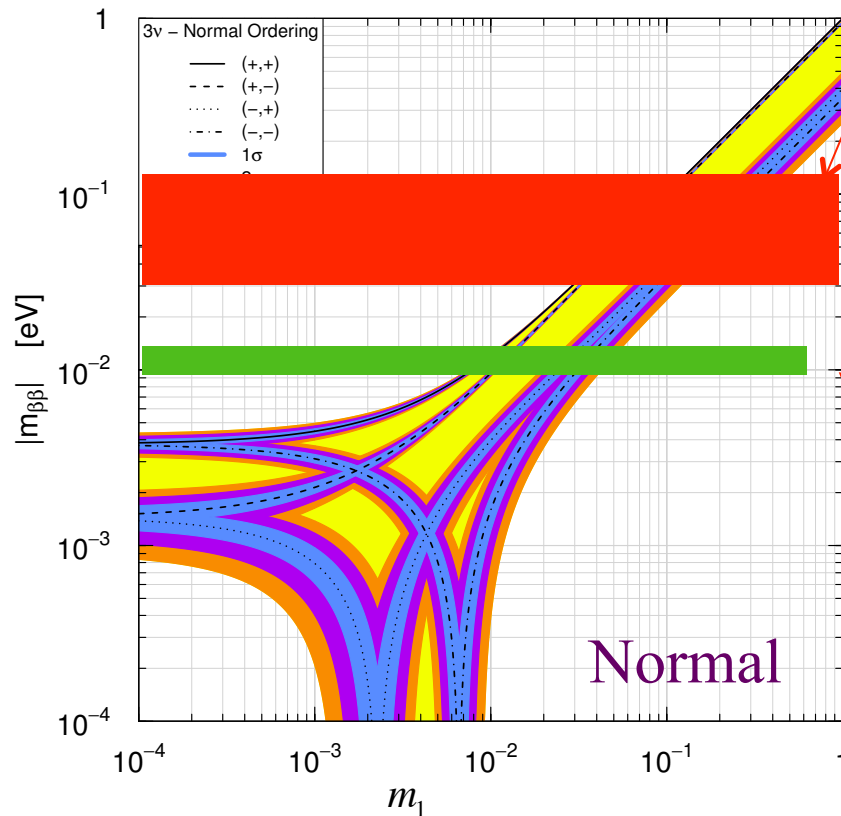
-0.0215 MeV⁻¹



Neutrino $\beta\beta$ effective mass

arxiv:1507.08204

KamLAND – Zen, PRL 117, 082503 (2016): ^{136}Xe



$$|m_{\beta\beta}| = \left| \sum_{k=1}^3 m_k U_{ek}^2 \right| = \left| c_{12}^2 c_{13}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3} \right|$$

$$\phi_2 = \alpha_2 - \alpha_1 \quad \phi_3 = -\alpha_1 - 2\delta$$

$$\Leftrightarrow T_{1/2}^{-1}(0\nu) = G^{0\nu}(Q_{\beta\beta}) \left[M^{0\nu}(0^+) \right]^2 (\eta_{0\nu})^2$$

$$\eta_{0\nu} = \frac{|m_{\beta\beta}|}{m_e}$$

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Shell Model Nuclear Matrix Elements

$$M_S^{0\nu} = \sum_{\substack{J, p < p' \\ n < n' \\ p < n}} (\Gamma) \left\langle 0_f^+ \left| \left[\left(a_p^+ a_{p'}^+ \right)^J \left(\tilde{a}_n, \tilde{a}_n \right)^J \right]^0 \right| 0_i^+ \right\rangle \left\langle p p'; J \left| \int q^2 dq \left[\hat{S} \frac{h(q) j_\kappa(qr) G_{FS}^2 f_{SRC}^2}{q(q + \langle E \rangle)} \tau_1 \tau_2 \right] n n'; J \right\rangle_{as} - \text{closure}$$

Short range correlations (SRC): $f_{SRC} = 1 - c e^{ar^2} (1 - br^2)$

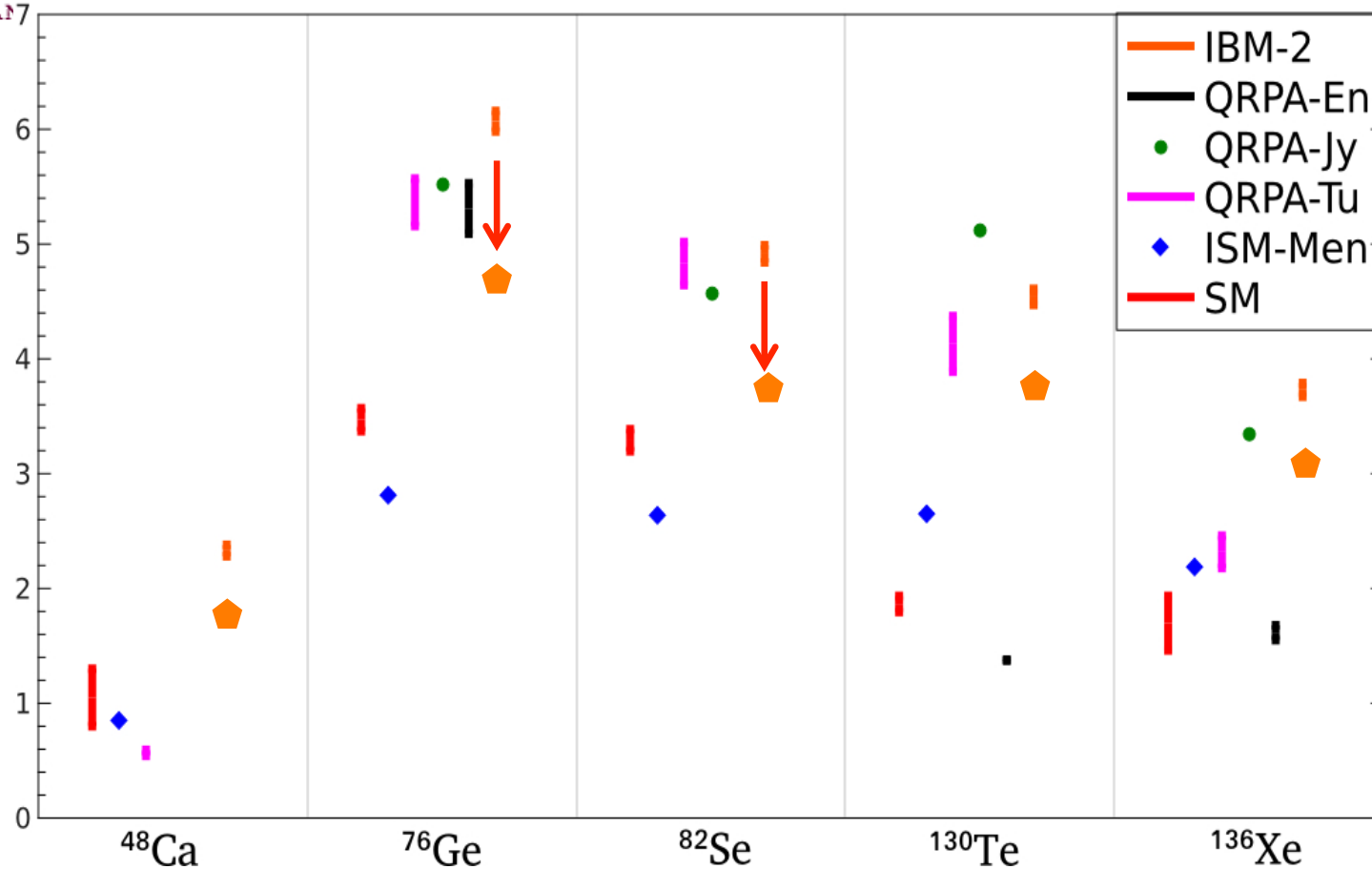
$$M^{0\nu} = M_{GT}^{0\nu} - (g_V / g_A)^2 M_F^{0\nu} + M_T^{0\nu}$$

$$\hat{S} = \begin{cases} \sigma_1 \tau_1 \sigma_2 \tau_2 & \text{Gamow - Teller (GT)} \\ \tau_1 \tau_2 & \text{Fermi (F)} \\ [3(\vec{\sigma}_1 \cdot \hat{n})(\vec{\sigma}_2 \cdot \hat{n}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)] \tau_1 \tau_2 & \text{Tensor (T)} \end{cases}$$

TABLE II. Parameters for the short-range correlation (SRC) parametrization of Eq. (11).

	SRC	a	b	c
MS SRC	Miller-Spencer	1.10	0.68	1.00
CDB SRC	CD-Bonn	1.52	1.88	0.46
AV18 SRC	AV18	1.59	1.45	0.92

NME for the light-neutrino exchange mechanism



IBA-2 J. Barea, J. Kotila, and F. Iachello, Phys. Rev. C **87**, 014315 (2013). → IBM-2 PRC **91**, 034304 (2015)

QRPA-En M. T. Mustonen and J. Engel, Phys. Rev. C **87**, 064302 (2013).

QRPA-Jy J. Suhonen, O. Civitarese, Phys. NPA **847** 207–232 (2010).

QRPA-Tu A. Faessler, M. Gonzalez, S. Kovalenko, and F. Simkovic, arXiv:1408.6077

ISM-Men J. Menéndez, A. Poves, E. Caurier, F. Nowacki, NPA **818** 139–151 (2009).

SM M. Horoi et. al. PRC **88**, 064312 (2013), PRC **89**, 045502 (2014), PRC **89**, 054304 (2014), PRC **90**, 051301(R) (2014), PRC **91**, 024309 (2015), PRL **110**, 222502 (2013), PRL **113**, 262501(2014).

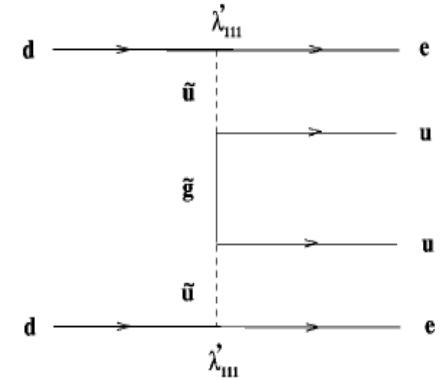
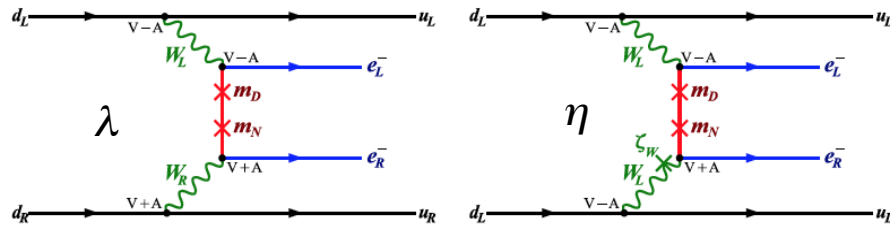
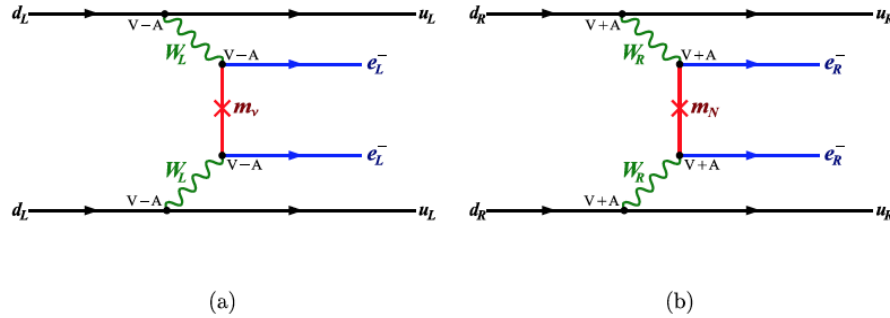
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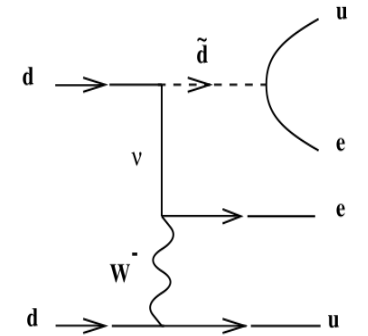
Other models: Left-Right symmetric model and SUSY R-parity violation

DAS *et al.*

PHYSICAL REVIEW D 86, 055006 (2012)



Gluino exchange



Squark
exchange

$$\left[T_{1/2}^{0\nu} \right]^{-1} = G_{01} g_A^4 \left| \eta_{0\nu} M_{0\nu} + (\eta_{N_R}^L + \eta_{N_R}^R) M_{0N} + \eta_{\tilde{q}} M_{\tilde{q}} + \eta_{\lambda'} M_{\lambda'} + \eta_{\lambda} X_{\lambda} + \eta_{\eta} X_{\eta} \right|^2.$$

(e)

M. Horoi, A. Neacsu, PRD 93, 113014 (2016)

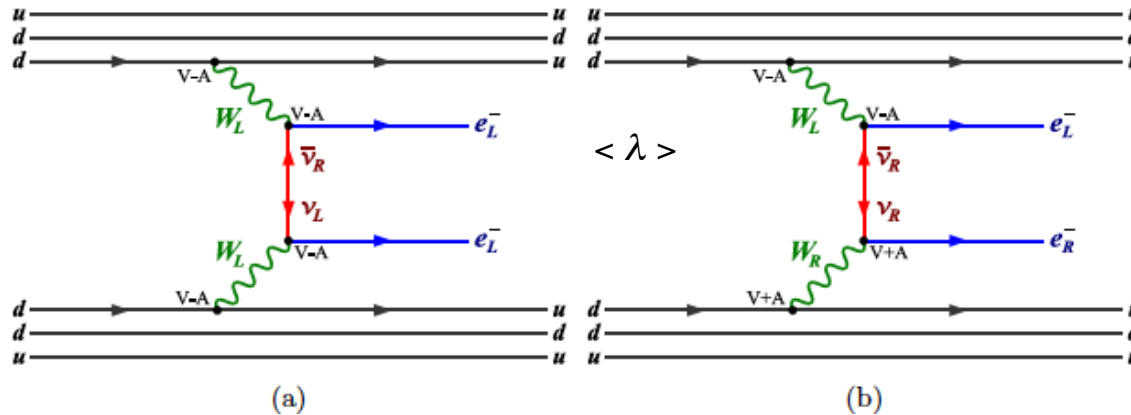
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DBD signals from different mechanisms

R. Arnold et al.: Probing New Physics Models of Neutrinoless Double Beta Decay with SuperNEMO

arXiv:1005.1241



$$\left[T_{1/2}^{0\nu} \right]^{-1} = \left| M_{GT}^{(0\nu)} \right|^2 \left\{ C_{\nu^2} + C_{\nu\lambda} \cos\phi_1 + C_{\nu\eta} \cos\phi_2 + C_{\lambda^2} + C_{\eta^2} + C_{\lambda\eta} \cos(\phi_1 - \phi_2) \right\},$$

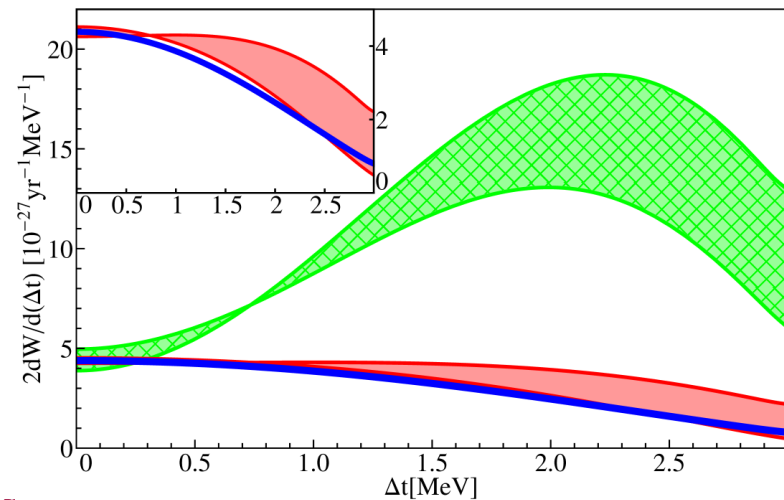
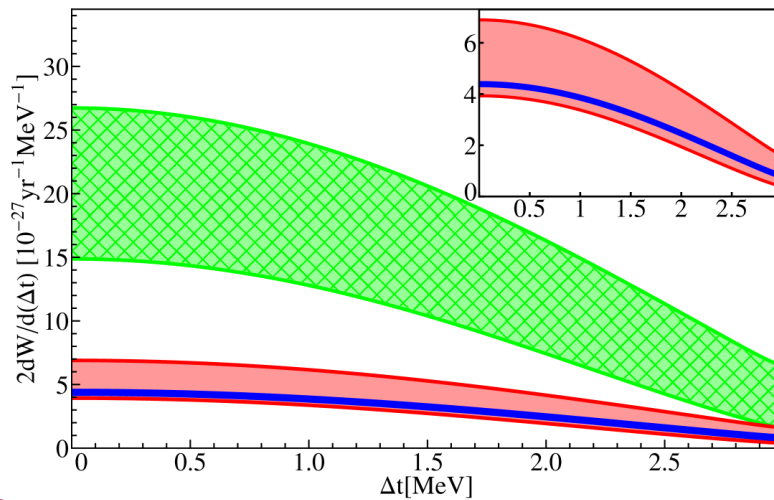
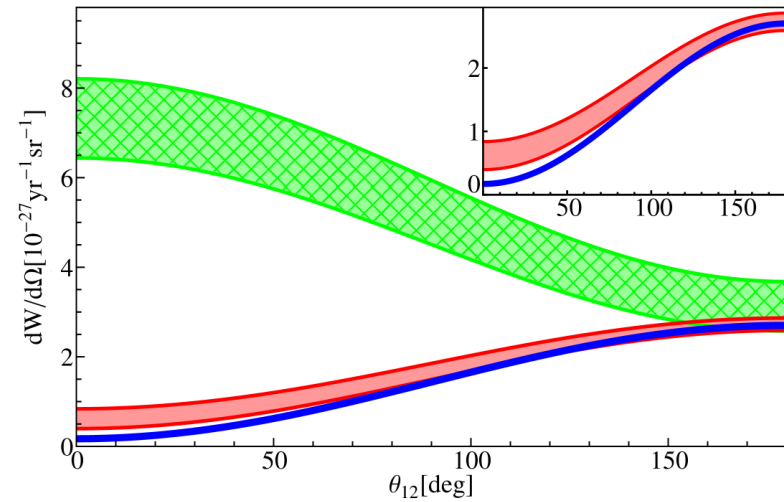
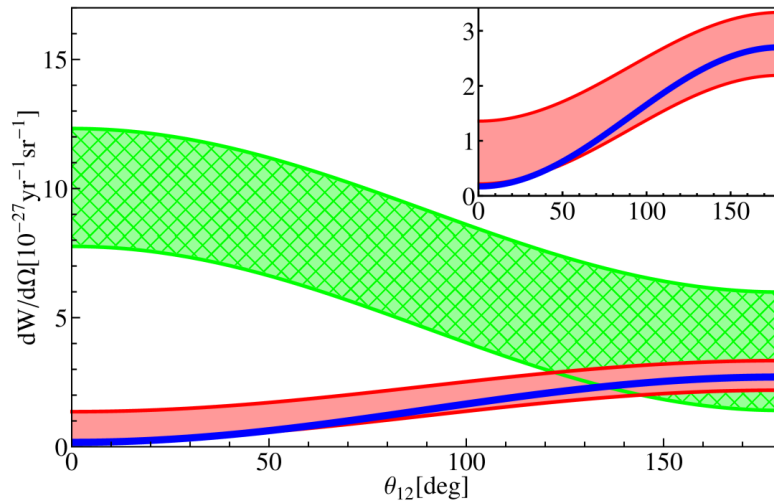
$$\frac{d^2 W_{0^+ \rightarrow 0^+}^{0\nu}}{d\epsilon_1 d\cos\theta_{12}} = \frac{a_{0\nu} \omega_{0\nu}(\epsilon_1)}{2(m_e R)^2} [A(\epsilon_1) + B(\epsilon_1) \cos\theta_{12}]$$

$$\frac{2dW_{0^+ \rightarrow 0^+}^{0\nu}}{d(\Delta t)} = \frac{2a_{0\nu}}{(m_e R)^2} \frac{\omega_{0\nu}(\Delta t)}{m_e c^2} A(\Delta t)$$

$$t = \epsilon_{e1} - \epsilon_{e2}$$

λ and η mechanisms (^{82}Se): look for green

$\langle \lambda \rangle$ dominates



Two Non-Interfering Mechanisms

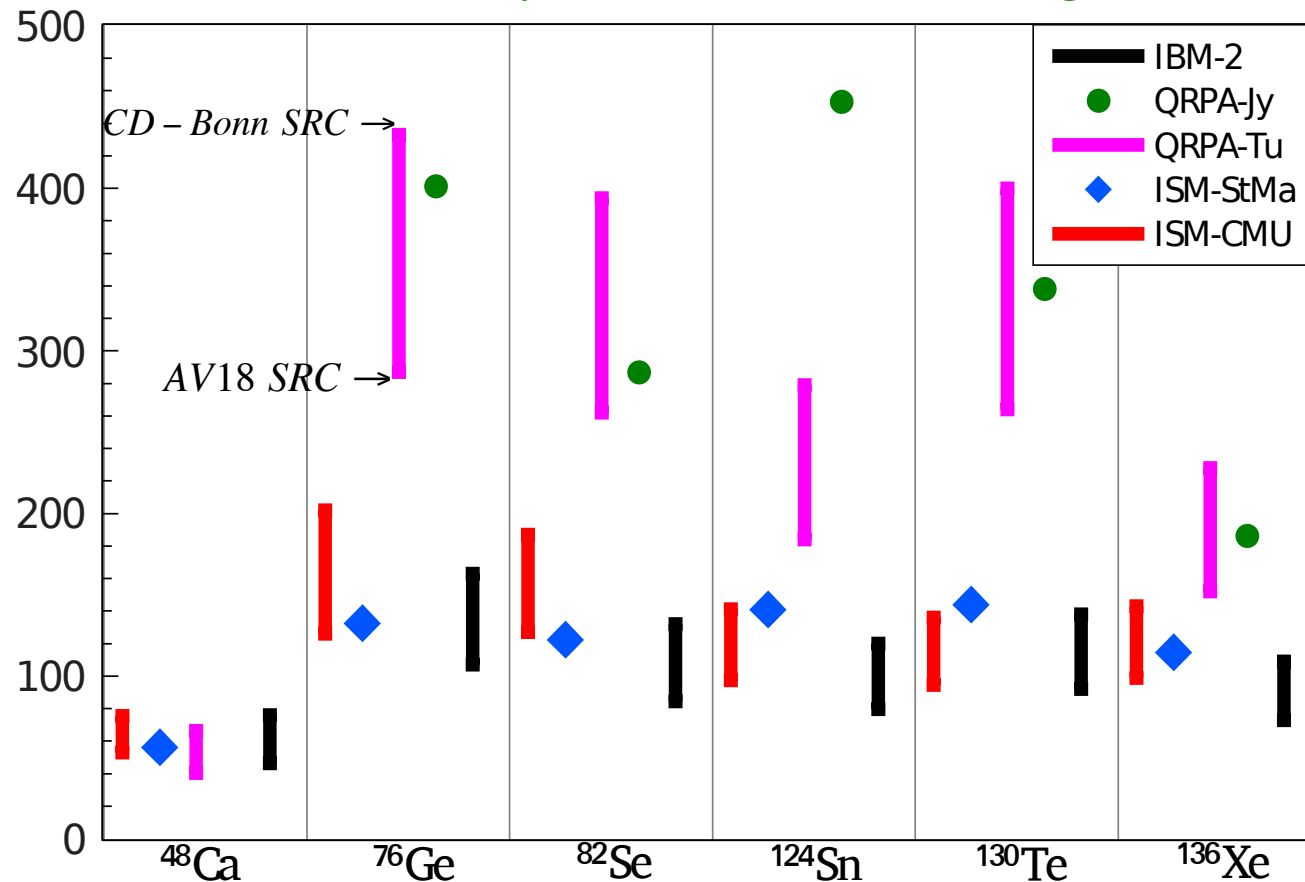
$$r(\nu / N) \equiv T_{1/2}^{\nu/N}(1) / T_{1/2}^{\nu/N}(2) = \frac{G_{01}^{0\nu}(2) |M^{0\nu/N}(2)|^2}{G_{01}^{0\nu}(1) |M^{0\nu/N}(1)|^2}$$

	Ge/Se		Ge/Te		Ge/Xe		Se/Te		Se/Xe		Te/Xe	
	Ge	Se	Ge	Te	Ge	Xe	Se	Te	Se	Xe	Te	Xe
$G_{01}^{0\nu} \times 10^{14}$	0.237	1.018	0.237	1.425	0.237	1.462	1.018	1.425	1.018	1.462	1.425	1.462
$M^{0\nu}(1/2)$	3.57	3.39	3.57	1.93	3.57	1.76	3.39	1.93	3.39	1.76	1.93	1.76
$M^{0N}(1/2)$	202	187	202	136	202	143	187	136	187	143	136	143
$T_{1/2}^{\nu}(1)/T_{1/2}^{\nu}(2)$	3.87		1.76		1.50		0.45		0.39		0.85	
$T_{1/2}^N(1)/T_{1/2}^N(2)$	3.68		2.73		3.09		0.74		0.84		1.13	
$R(N/\nu)$ present	0.95		1.55		2.06		1.63		2.17		1.33	
$R(N/\nu)$ [45]	1.02		1.39		1.42		1.36		1.39		1.03	

$$R(N / \nu) = r(N) / r(\nu)$$

Heavy neutrino-exchange NME

M_{0N}



IBA-2 J. Barea, J. Kotila, and F. Iachello, Phys. Rev. C **87**, 014315 (2013).

QRPA-Tu A. Faessler, M. Gonzalez, S. Kovalenko, and F. Simkovic, arXiv:1408.6077.

QRPA-Jy J. Hivarynen and J. Suhonen, PRC **91**, 024613 (2015), **ISM-StMa** J. Menendez, private communication.

ISM-CMU M. Horoi et. al. PRC **88**, 064312 (2013), PRC **90**, PRC **89**, 054304 (2014), PRC **91**, 024309 (2015), PRL **110**, 222502 (2013).

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Towards an effective $0\nu\text{DBD}$ operator

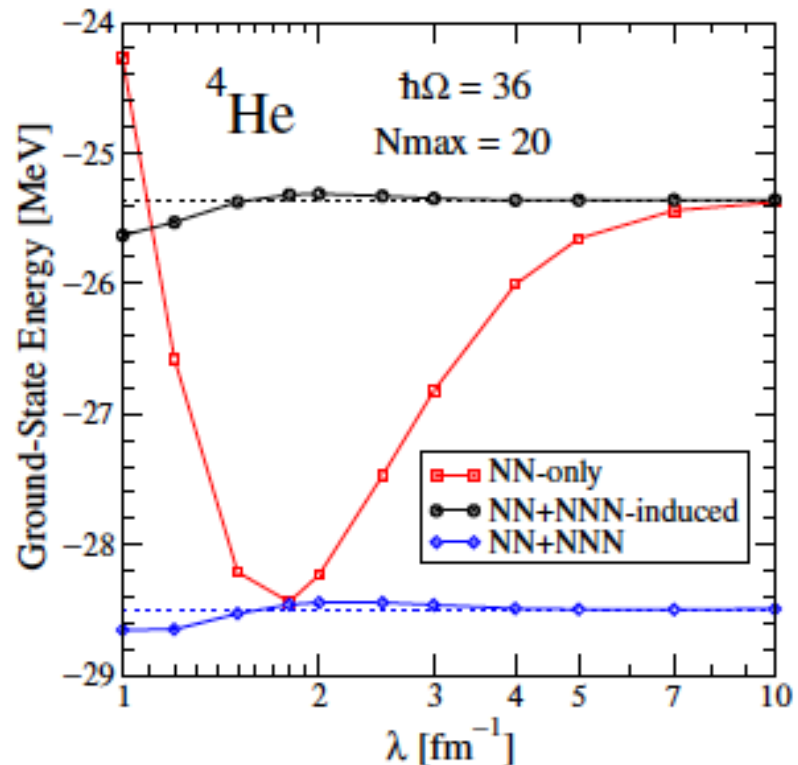
Similarity Renormalization Group (SRG) evolution

$$H_\lambda = U_\lambda H_{\lambda=\infty} U_\lambda^\dagger$$

$$\frac{dH_\lambda}{d\lambda} = -\frac{4}{\lambda^5} [[G, H_\lambda], H_\lambda]$$

$$O_\lambda = U_\lambda O_{\lambda=\infty} U_\lambda^\dagger$$

N3LO 500

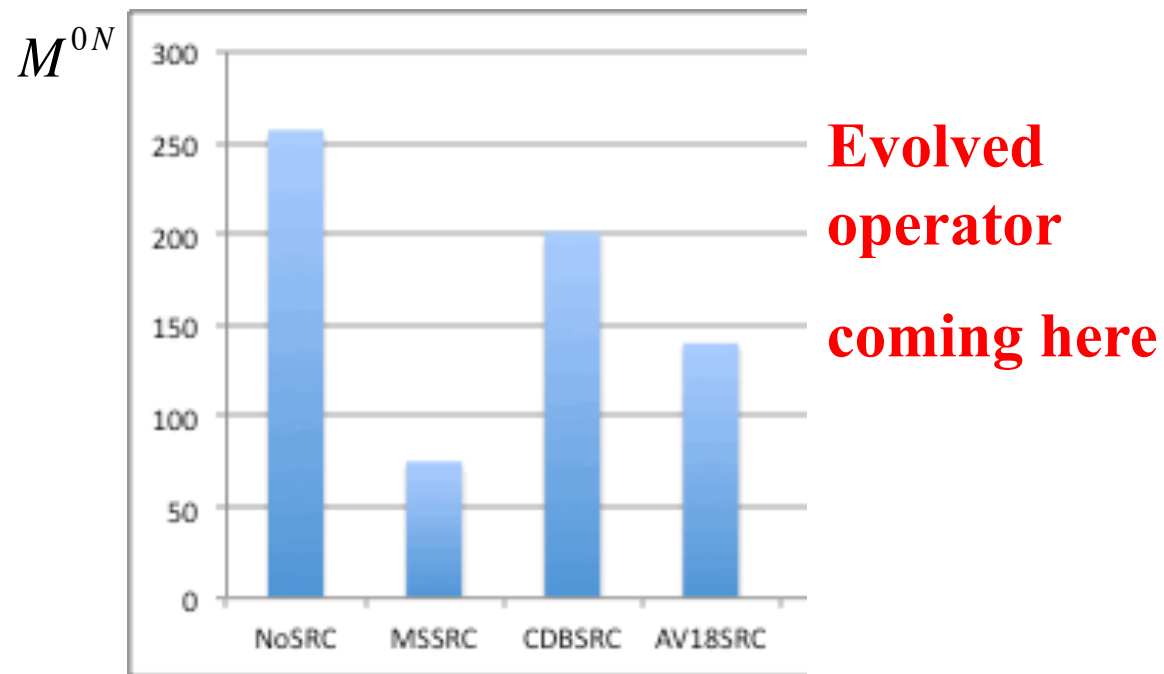


arXiv:1302.5473

Towards an effective $0\nu\text{DBD}$ operator: heavy neutrino-exchange NME

$$O_{\lambda} = U_{\lambda} O_{\lambda=\infty} U_{\lambda}^{\dagger}$$

^{76}Ge

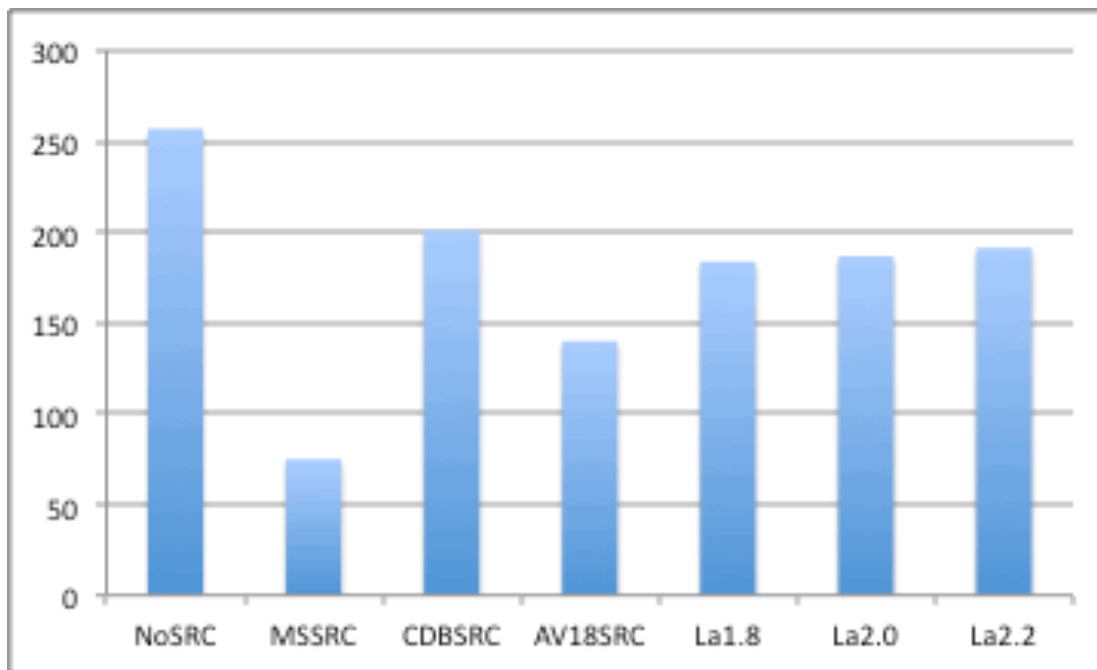


Towards an effective 0ν DBD operator: heavy neutrino-exchange NME

$$O_{\lambda} = U_{\lambda} O_{\lambda=\infty} U_{\lambda}^{\dagger}$$

^{76}Ge

M^{0N}

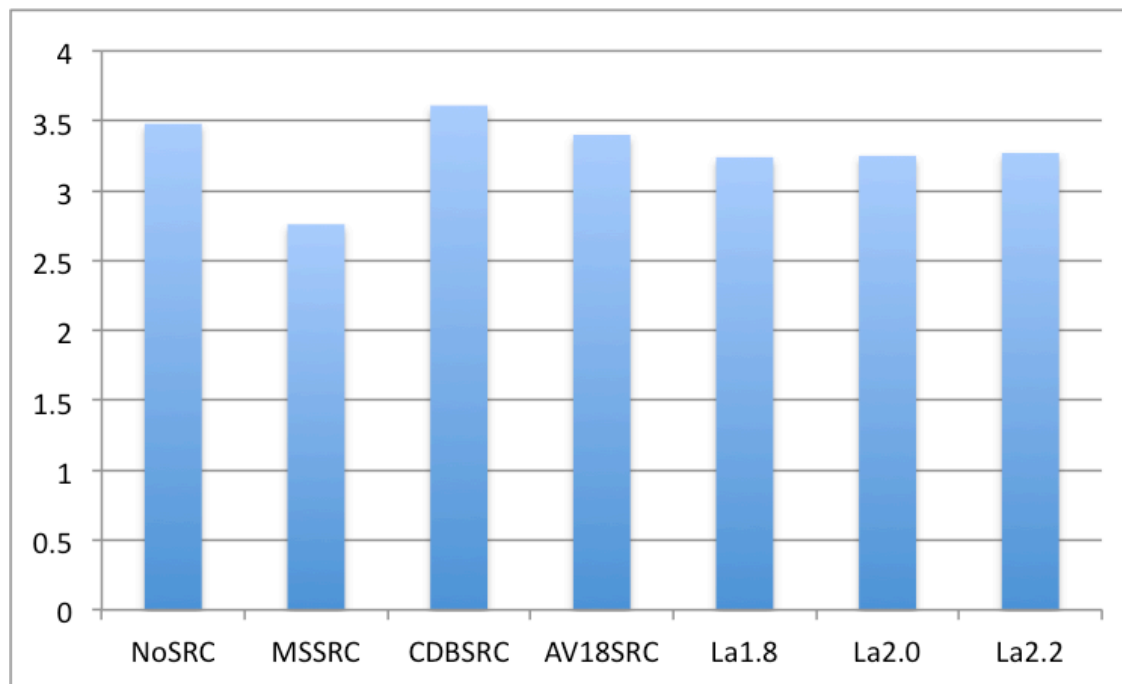


Towards an effective 0ν DBD operator: light neutrino-exchange NME

$$O_{\lambda} = U_{\lambda} O_{\lambda=\infty} U_{\lambda}^{\dagger}$$

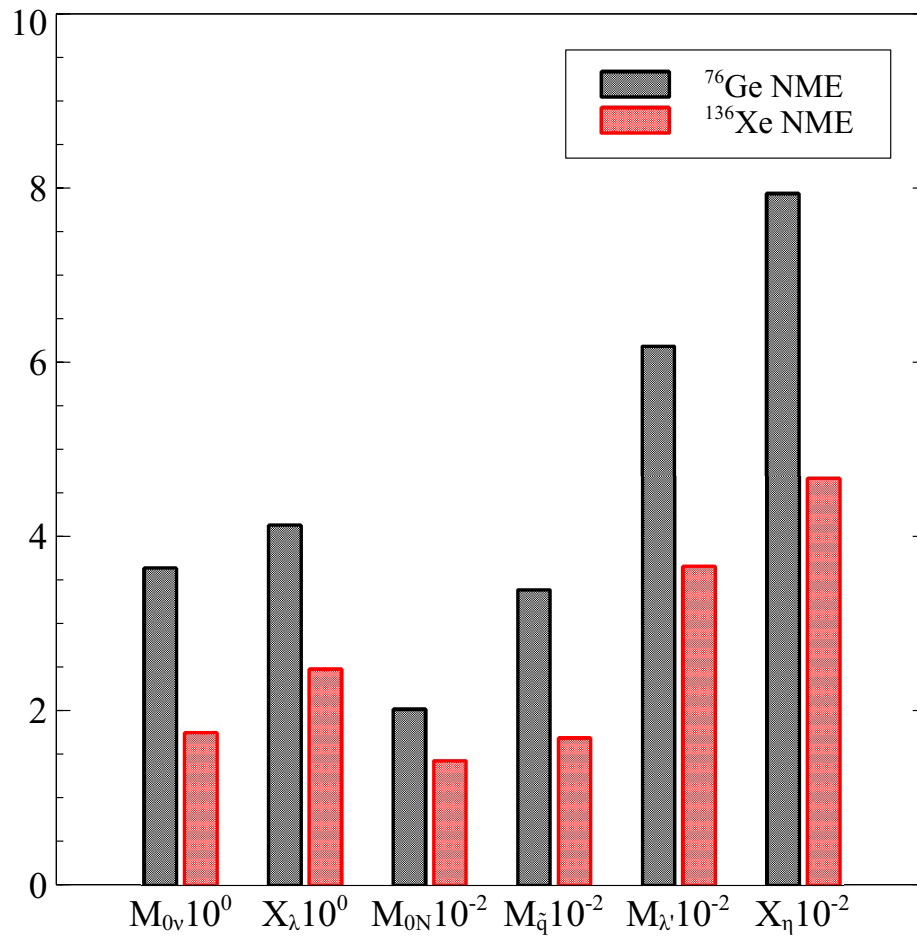
^{76}Ge

$M^{0\nu}$

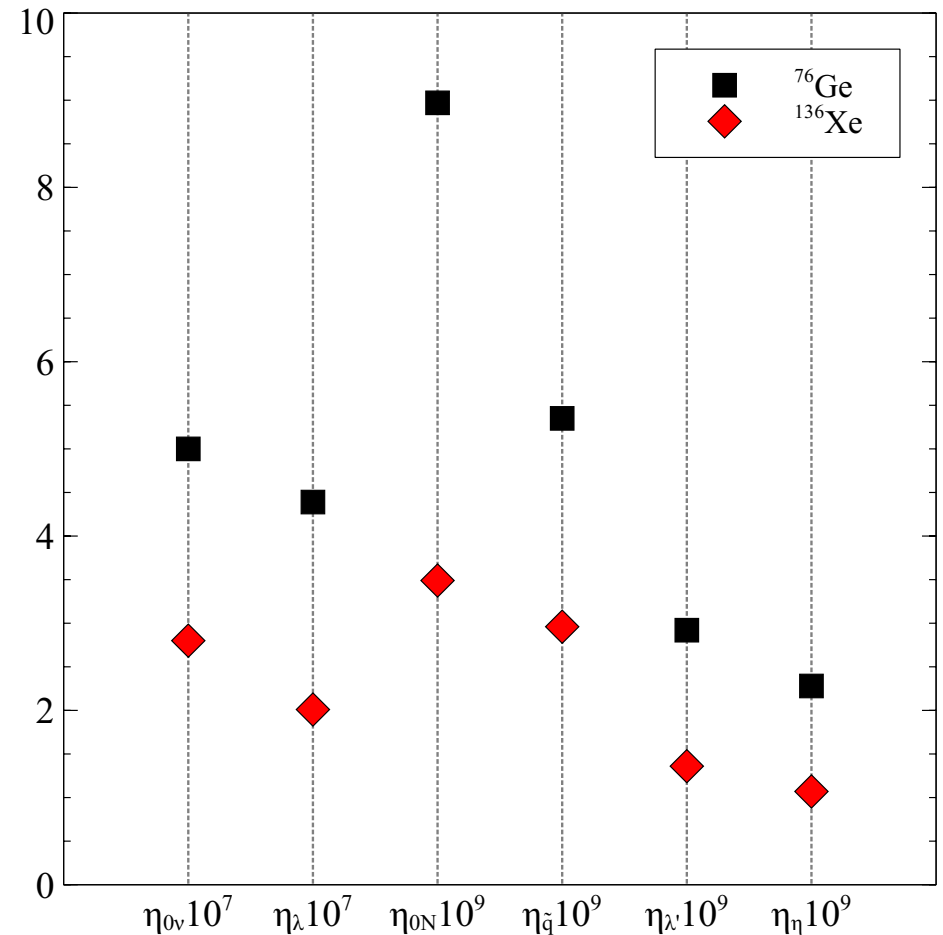


One mechanism dominance

$$\left[T_{1/2}^{0\nu}\right]^{-1} = G_{01} g_A^4 \left| \eta_{0\nu} M_{0\nu} + (\eta_{N_R}^L + \eta_{N_R}^R) M_{0N} + \eta_{\tilde{q}} M_{\tilde{q}} + \eta_{\lambda'} M_{\lambda'} + \eta_{\lambda} X_{\lambda} + \eta_{\eta} X_{\eta} \right|^2.$$



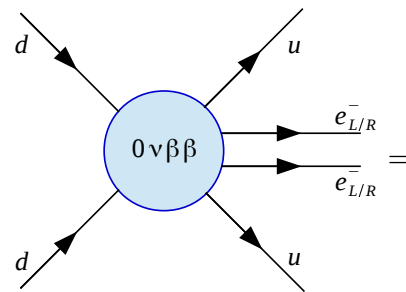
$$T_{1/2}^{0\nu}(^{76}\text{Ge}) > 5 \times 10^{25} \text{ years} \quad T_{1/2}^{0\nu}(^{136}\text{Xe}) > 1.1 \times 10^{26} \text{ years}$$



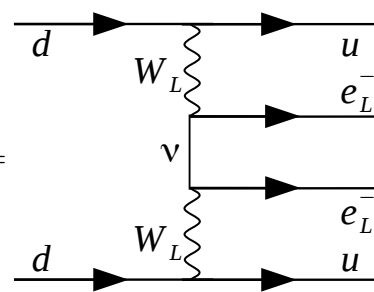
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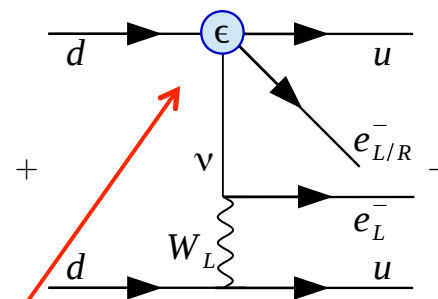
Effective field theory approach



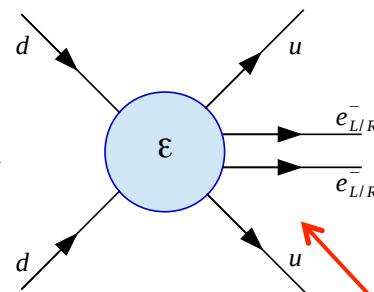
(a) The generic $0\nu\beta\beta$ decay diagram at the quark-level.



(b) Light left-handed neutrino exchange diagram.



(c) The long-range part of the $0\nu\beta\beta$ diagram.

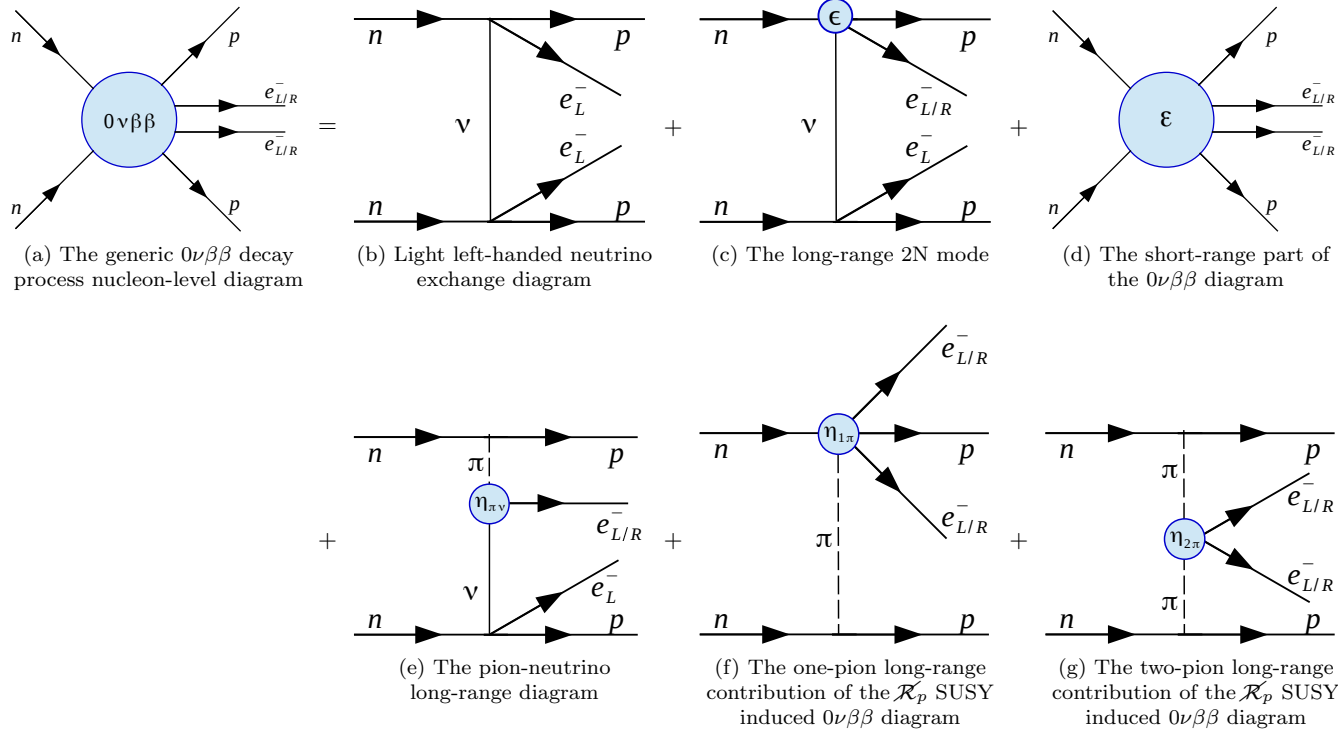


(d) The short-range part of the $0\nu\beta\beta$ diagram.

$$\mathcal{L}_6 = \frac{G_F}{\sqrt{2}} \left[j_{V-A}^\mu J_{V-A,\mu}^\dagger + \sum_{\alpha,\beta}^* \epsilon_{\alpha\beta}^\beta j_\beta J_\alpha^\dagger \right]$$

$$\mathcal{L}_9 = \frac{G_F^2}{2m_p} \left[\epsilon_1 J J j + \epsilon_2 J^{\mu\nu} J_{\mu\nu} j + \epsilon_3 J^\mu J_\mu j \right. \\ \left. + \epsilon_4 J^\mu J_{\mu\nu} j^\nu + \epsilon_5 J^\mu J j_\mu \right],$$

Effective field theory after hadronization



$$\left[T_{1/2}^{0\nu} \right]^{-1} = g_A^4 \left[\sum_i |\mathcal{E}_i|^2 \mathcal{M}_i^2 + \text{Re} \left[\sum_{i \neq j} \mathcal{E}_i \mathcal{E}_j \mathcal{M}_{ij} \right] \right]$$

$$\mathcal{E}_{2-7} = \{ \epsilon_{V-A}^{V+A}, \epsilon_{V+A}^{V+A}, \epsilon_{S \pm P}^{S+P}, \epsilon_{TL}^{\tilde{T}R}, \epsilon_{\tilde{T}R}^{\tilde{T}R}, \eta_{\pi\nu} \}$$

$$\mathcal{E}_{8-15} = \{ \epsilon_1, \epsilon_2, \epsilon_3^{LLz(RRz)}, \epsilon_3^{LRz(RLz)}, \epsilon_4, \epsilon_6, \eta_{1\pi}, \eta_{2\pi} \}$$

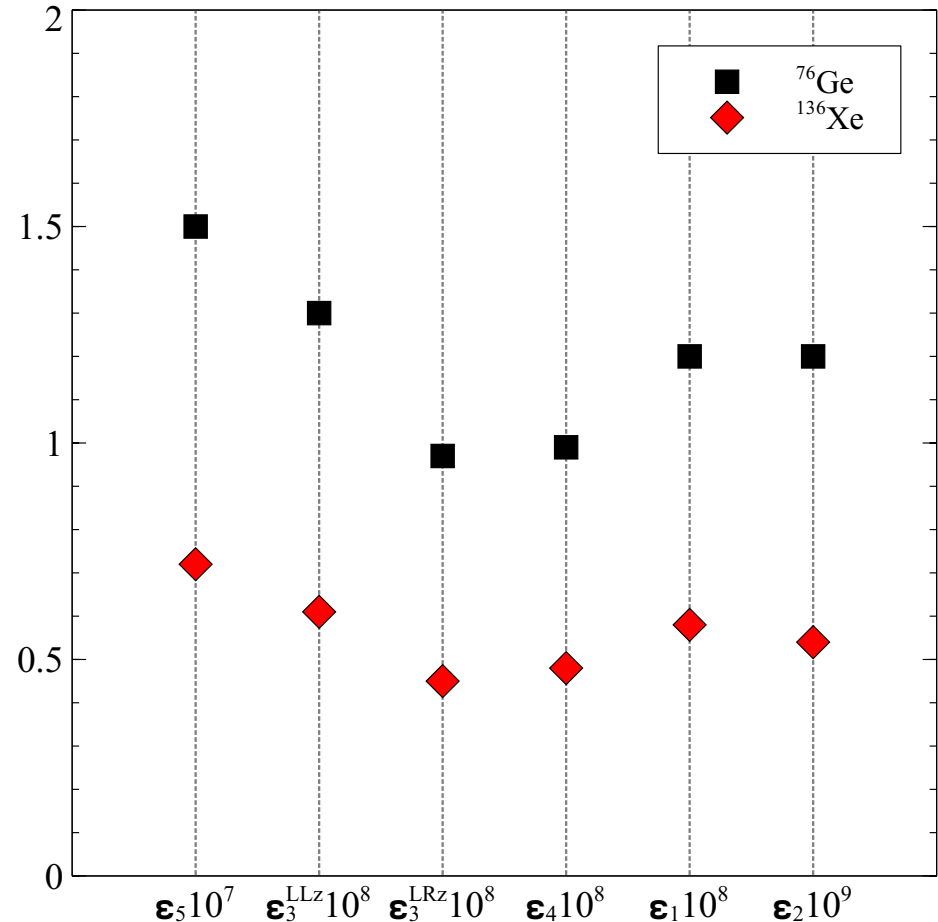
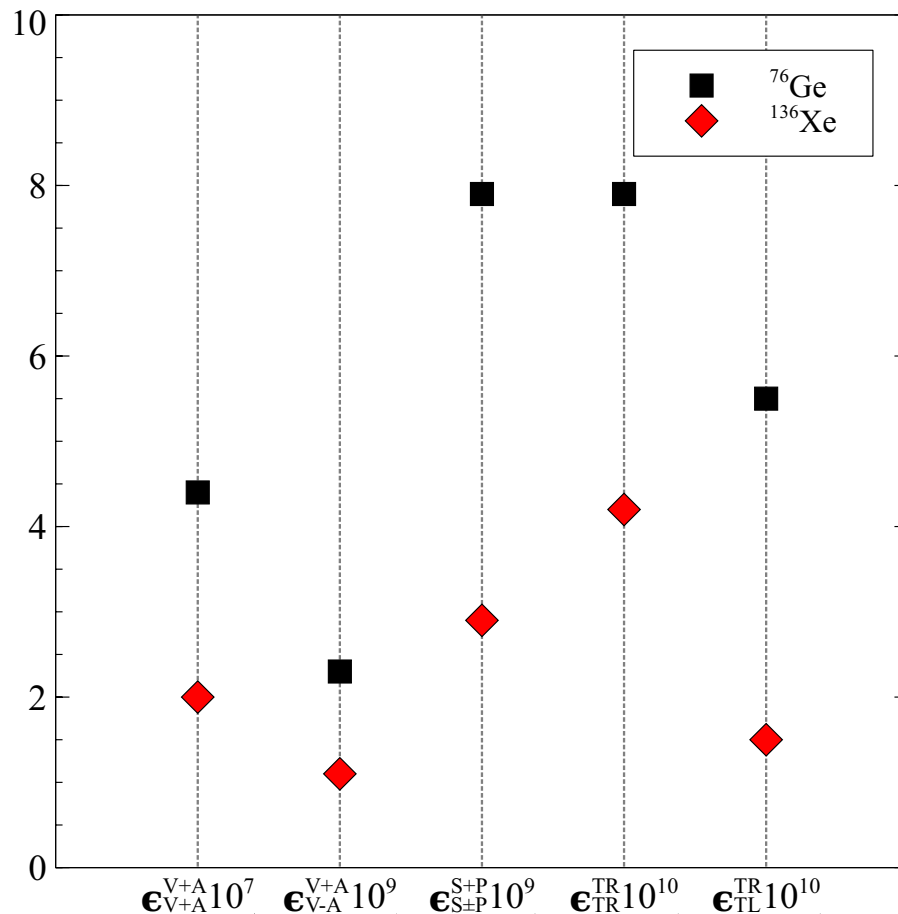
One coupling dominance

$$\left[T_{1/2}^{0\nu}\right]^{-1} = g_A^4 \left[\sum_i |\mathcal{E}_i|^2 \mathcal{M}_i^2 + \text{Re} \left[\sum_{i \neq j} \mathcal{E}_i \mathcal{E}_j^* \mathcal{M}_{ij} \right] \right]$$



$$\mathcal{E}_{2-7} = \{\epsilon_{V-A}^{V+A}, \epsilon_{V+A}^{V+A}, \epsilon_{S \pm P}^{S+P}, \epsilon_{TL}^{TR}, \epsilon_{TR}^{TR}, \eta_{\pi\nu}\}$$

$$\mathcal{E}_{8-15} = \{\epsilon_1, \epsilon_2, \epsilon_3^{LLz(RRz)}, \epsilon_3^{LRz(RLz)}, \epsilon_4, \epsilon_6, \eta_{1\pi}, \eta_{2\pi}\}$$



MEDEX17, May 29,
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M. Horoi CMU

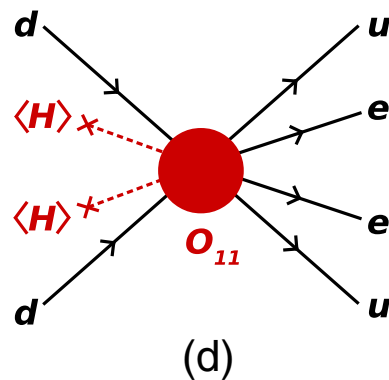
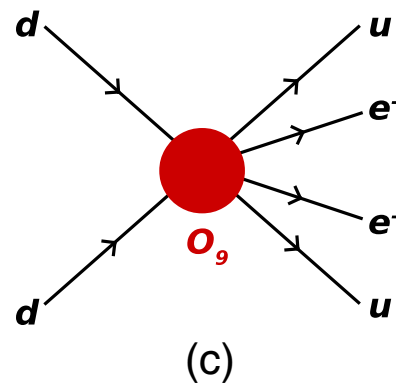
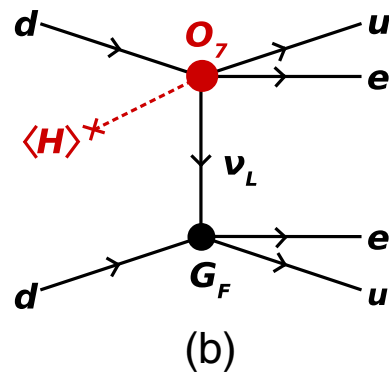
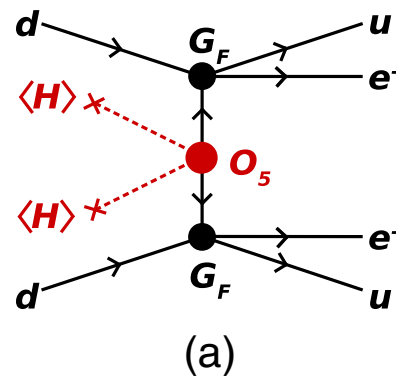
$$T_{1/2}^{0\nu}({}^{76}\text{Ge}) > 5 \times 10^{25} \text{ years} \quad T_{1/2}^{0\nu}({}^{136}\text{Xe}) > 1.1 \times 10^{26} \text{ years}$$

Consequences: - scales for new physics

- baryogenesis via leptogenesis

PHYSICAL REVIEW D **92**, 036005 (2015)

$$\mathcal{L}_D = \frac{g}{\Lambda_D^{D-4}} \mathcal{O}_D$$



$$m_e \bar{\epsilon}_5 = \frac{g^2 v^2}{\Lambda_5}, \quad \frac{G_F \bar{\epsilon}_7}{\sqrt{2}} = \frac{g^3 v}{2 \Lambda_7^3},$$

$$\frac{G_F \bar{\epsilon}_9}{2 m_p} = \frac{g^4}{\Lambda_9^5}, \quad \frac{G_F \bar{\epsilon}_{11}}{2 m_p} = \frac{g^6 v^2}{\Lambda_{11}^7}$$

$$g \approx 1 \quad v = 174 \text{ GeV (Higgs expectation value)}$$

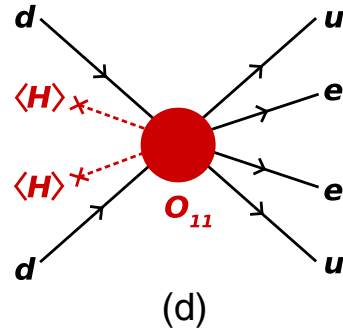
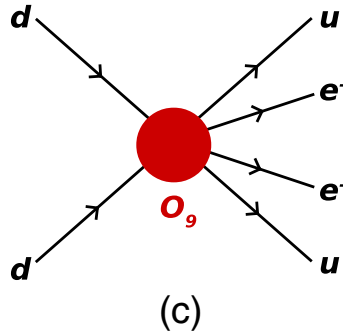
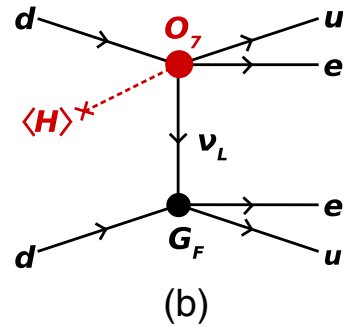
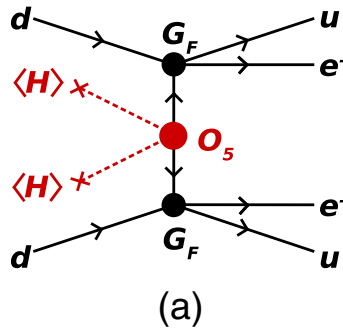
\mathcal{O}_D	$\bar{\epsilon}_D$	Λ_D
\mathcal{O}_5	2.8×10^{-7}	2.12×10^{14}
\mathcal{O}_7	2.0×10^{-7}	3.75×10^4
\mathcal{O}_9	1.5×10^{-7}	2.48×10^3
\mathcal{O}_{11}	1.5×10^{-7}	1.16×10^3

Consequences: - scales for new physics

- baryogenesis via leptogenesis

PHYSICAL REVIEW D **92**, 036005 (2015)

$$\mathcal{L}_D = \frac{g}{(\Lambda_D)^{D-4}} \mathcal{O}_D$$



$$m_e \bar{\epsilon}_5 = \frac{g^2 (yv)^2}{\Lambda_5}, \quad \frac{G_F \bar{\epsilon}_7}{\sqrt{2}} = \frac{g^3 (yv)}{2(\Lambda_7)^3},$$

$$\frac{G_F \bar{\epsilon}_9}{2m_p} = \frac{g^4}{(\Lambda_9)^5}, \quad \frac{G_F \bar{\epsilon}_{11}}{2m_p} = \frac{g^6 (yv)^2}{(\Lambda_{11})^7}$$

TABLE VIII. The BSM effective scale (in GeV) for different dimension-D operators at the present ^{136}Xe half-life limit (Λ_D^0) and for $T_{1/2} \approx 1.1 \times 10^{28}$ years (Λ_D).

\mathcal{O}_D	$\bar{\epsilon}_D$	$\Lambda_D^0(y=1)$	$\Lambda_D^0(y=y_e)$	$\Lambda_D(y=y_e)$
\mathcal{O}_5	$2.8 \cdot 10^{-7}$	$2.12 \cdot 10^{14}$	1904	19044
\mathcal{O}_7	$2.0 \cdot 10^{-7}$	$3.75 \cdot 10^4$	541	1165
\mathcal{O}_9	$1.5 \cdot 10^{-7}$	$2.47 \cdot 10^3$	2470	3915
\mathcal{O}_{11}	$1.5 \cdot 10^{-7}$	$1.16 \cdot 10^3$	31	43

$$g \approx 1 \quad v = 174 \text{ GeV} \text{ (Higgs expectation value)}$$

$$y_e = 3 \times 10^{-6} \text{ electron mass Yukawa}$$

Summary

- The physics of the neutrinos is very exciting and offers a lot of research opportunities.
- Double beta decay (DBD), if observed, will represent a big step forward in our understanding of the neutrinos, and of physics beyond the Standard Model. A Nobel prize may be awarded for its discovery.
- The physics learned from DBD is complementary to that learned from Large Hadron Collider (future colliders).
- Better nuclear matrix elements and effective DBD operators are needed, especially for the short range mechanisms. And we are working hard for that!

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