

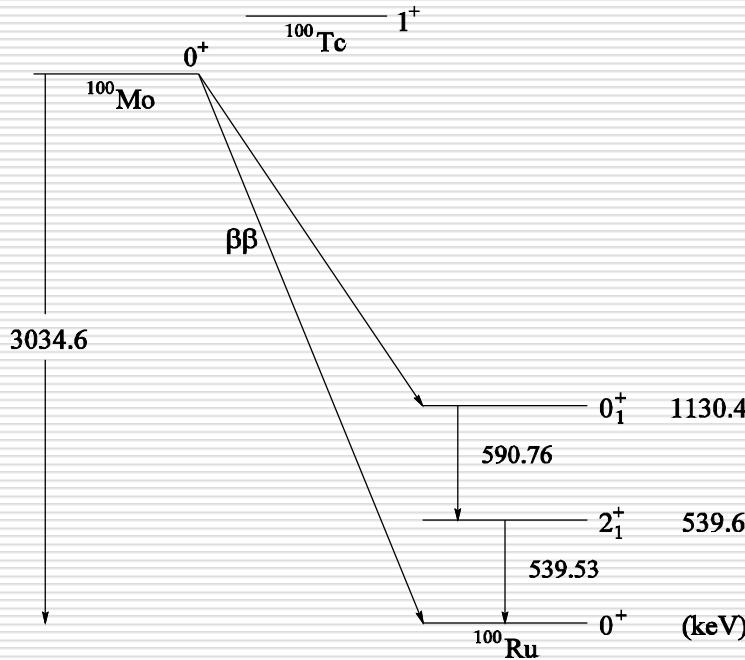
DOUBLE BETA DECAY TO THE EXCITED STATES: REVIEW

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OUTLINE

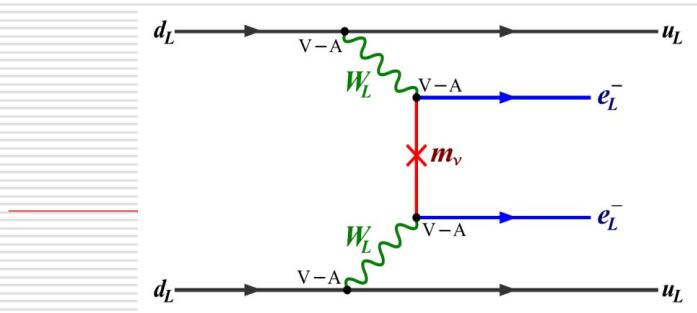
- Introduction
 - **$2\beta^-(2\nu)$** -decay to the excited states
 - **$2\beta^-(0\nu)$** -decay to the excited states
 - **ECEC** to the excited states
 - Conclusion
-

1. Introduction



There are 35 candidates for
2 β -decay

$$\begin{aligned} W &\sim Q^5 (0\nu); W \sim Q^7 (0\nu\chi^0) \\ W &\sim Q^{11} (2\nu) \end{aligned}$$



1.1. Historical introduction

E. Fiorini (**1977, NEUTRINO'77**) – first time limit on **0⁺⁻-2⁺** decay in Ge-76 was obtained (as by-product for 0⁺⁻-0⁺ transition)*):

$$T_{1/2} (0\nu) > 3 \cdot 10^{21} \text{ y (68% C.L.)}$$

*) Of course, from geochemical experiments one can extract limits too.

1982 – first special experimental work to investigate $2\beta^-$ -decay to the excited states has been done:

E. Bellotti et al., Lett. Nuov. Cim. 33 (1982) 273.

(^{58}Ni , ^{76}Ge , ^{92}Mo , ^{100}Mo , ^{148}Nd , ^{150}Nd ;
Transitions to 2^+_1 , 0^+_1 , 2^+_2 , ... excited
states)

Limits on the level $(1.2\text{-}3.2)\cdot10^{21}$ y for
 ^{76}Ge and $\sim 10^{18}\text{-}10^{19}$ y for other
nuclei have been obtained.

1983-1988

- Many new results for **^{76}Ge (0^+ - 2^+)**. And even “evidence” of the decay on 2.5σ level ($T_{1/2} \approx 10^{22}$ y) has been obtained.
 - 3 experiments were done by **E. Norman** (^{50}Cr , ^{58}Ni , ^{64}Zn , ^{92}Mo , ^{94}Zr , ^{96}Zr , ^{96}Ru , ^{106}Cd , ^{116}Cd , ^{124}Sn ; natural samples).
Limits on the level $\sim \mathbf{10^{17}-10^{19}}$ y have been obtained.
-

1989-1990

- It was demonstrated that $2\beta(2\nu;0+-0+)$ -decay can be detected in ^{100}Mo , ^{96}Zr and ^{150}Nd by existing low-background HPGe detectors and new experiments were proposed (**A.S.B. preprint ITEP, 188-89, 1989; JETP Lett. 51 (1990) 207**).
 - ITEP-USC-PNL-UM experiment with **1 kg of ^{100}Mo** was started on 30 May 1990 (in Soudan mine).
-

Measurement was stopped in September'91

- First “positive” result was reported at a few International Conferences (Moriond’91, TAUP’91, WEIN’92,...)
- Final result was published in 1995

[PL B 345 (1995) 408]:

$$T_{1/2} = 6.1^{+1.8}_{-1.1} \cdot 10^{20} \text{ y}$$

1999 - 2-nd positive result for
 ^{100}Mo (ITEP-BORDEAUX);

2001 - 3-d positive result for ^{100}Mo (**ITEP-TUNL**);

2004 - 1-st positive result for **^{150}Nd**
(ITEP-BORDEAUX);

2007 - 4-th positive result for **^{100}Mo (NEMO-3);**

2010 - 5-th positive result for **^{100}Mo**
(ARMONIA)

2014 - 6-th positive result for **^{100}Mo**
(NEMO-3 - OBELIX);

2014 - 2-nd positive result for **^{150}Nd (TUNL).**

2015-2016

EXO-200, KamLAND-Zen, GERDA-II:

**Sensitivity to excited states for
 ^{136}Xe and ^{76}Ge is $\sim 10^{24}\text{-}10^{25}$ yr !!!**

1.2. Present motivation

- **2ν**-decay:

- nuclear spectroscopy;
- NME** problem;
- **g_A** problem;
- Checking of some “creasy” ideas
(“bosonic” neutrino, ...)

- **0ν**-decay:

- very nice signature (**2β-**);
 - distinguishing between the various **0νββ** mechanisms;
 - possible high sensitivity (**ECEC**; resonance conditions).
-

II. $2\beta^-$ (2v)-decay to the excited states

Table 1. 2v transition to 2_{+1}^+ excited state.

Nucleus	$E_{2\beta}$, keV	$T_{1/2}$, y Experiment	Theory, 2007 [1]	Theory, 2015 [2]
^{48}Ca	3279.4	$>1.8 \cdot 10^{20}$	$1.7 \cdot 10^{24}$	-
^{150}Nd	3037.4	$>2.2 \cdot 10^{20}$	-	$7.2 \cdot 10^{24}$ [3]
^{96}Zr	2577.6	$>7.9 \cdot 10^{19}$	$2.3 \cdot 10^{25}$	$(1.1-1.4) \cdot 10^{21}$ [4]
^{100}Mo	2494.9	$>2.5 \cdot 10^{21}$	$1.2 \cdot 10^{25}$	$2 \cdot 10^{22} - 10^{23}$

Table 1. (Continue)

^{82}Se	2221.4	$>1\cdot10^{22}$	$1.7\cdot10^{27}$	$(1.0\text{-}2.4)\cdot10^{24}$ [4]
^{130}Te	1991.7	$>2.8\cdot10^{21}$	$6.9\cdot10^{26}$	$(4.2\text{-}9.1)\cdot10^{23}$
^{136}Xe	1639.3	$>\mathbf{4.6\cdot10^{23}}$	$3.9\cdot10^{26}$	$1.6\cdot10^{25}\text{-}4.8\cdot10^{26}$
^{116}Cd	1519.9	$>2.3\cdot10^{21}$	$3.4\cdot10^{26}$	$(2.5\text{-}5.2)\cdot10^{24}$
^{76}Ge	1480	$>\mathbf{1.6\cdot10^{23}}$	$5.8\cdot10^{28}$	$(2.4\text{-}4.3)\cdot10^{26}$ [4]
^{124}Sn	1689.9	$>9.1\cdot10^{20}$	-	$(5.3\text{-}6.4)\cdot10^{24}$

Table 2. 2ν-decay to 0^+_1 excited state

Nucleus	$E_{2\beta}$, keV	$T_{1/2}$, y Experiment	Theory [2]	Theory [5-7] (PSF prediction)
^{150}Nd	2630.9	$=1.2^{+0.3}_{-0.2} \cdot 10^{20}$	-	
^{96}Zr	2207.7	$>3.1 \cdot 10^{20}$	$(2.4-2.7) \cdot 10^{21}$	$(2.7-3.8) \cdot 10^{21}$ $(\sim 10^{21})$
^{100}Mo	1903.7	$=6.7^{+0.5}_{-0.4} \cdot 10^{20}$	$8.1 \cdot 10^{21}$ - $4.1 \cdot 10^{22}$	$2.1 \cdot 10^{21}$ $1.6 \cdot 10^{21}$ [8]
^{82}Se	1510.3	$>3.4 \cdot 10^{22}$	-	$(1.5-3.3) \cdot 10^{21}$ $(\sim 4 \cdot 10^{22})$
^{48}Ca	1265.7	$>1.5 \cdot 10^{20}$	-	-

Table 2. (Continue)

^{124}Sn	1131	$>1.1 \cdot 10^{21}$	-	-
^{116}Cd	1056.6	$>2.0 \cdot 10^{21}$	$(1.6\text{-}3.3) \cdot 10^{24}$	$1.1 \cdot 10^{21} \text{---} 1.1 \cdot 10^{22}$ $(\sim 10^{23})$
^{76}Ge	916.7	$>3.7 \cdot 10^{23}$	-	$4.5 \cdot 10^{21} \text{---} 3.1 \cdot 10^{23}$ $(\sim 10^{24})$
^{136}Xe	878.8	$>8.3 \cdot 10^{23}$	$(1.3\text{-}8.9) \cdot 10^{23}$	$2.5 \cdot 10^{21} \text{---} 6.3 \cdot 10^{21}$ $(\sim 10^{25})$
^{130}Te	734	$>1.3 \cdot 10^{23}$	$7.2 \cdot 10^{23}$ - $1.6 \cdot 10^{24}$	- $(\sim 2 \cdot 10^{25})$

References

- [1] A.A. Raduta and C.M. Raduta, Phys. Lett. B 647 (2007) 265.
 - [2] P. Pirinen and J. Suhonen, Phys. Rev. C 91 (2015) 054309.
 - [3] J.G. Hirsch et al., Nucl. Phys. A 589 (1995) 445.
 - [4] J. Schwieger et al., Phys. Rev. C 57 (1998) 1738.
 - [5] M. Aunola and J. Suhonen, Nucl. Phys. A 602 (1996) 133.
 - [6] J. Toivanen and J. Suhonen, Phys. Rev. C 55 (1997) 2314.
 - [7] S. Stoica and I. Mihut, Nucl. Phys. A 602 (1996) 197.
 - [8] J.G. Hirsch et al., Phys. Rev. C 51 (1995) 2252.
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Table 3. Present “positive” results on $2\beta(2\nu)$ decay of ^{100}Mo to the first 0^+ excited state of ^{100}Ru

$T_{1/2}$, y; $\times 10^{20}$	N	S/B	Year, method
$6.1^{+1.8}_{-1.1}$	133	~ 1/7	1995, HPGe [9]
$9.3^{+2.8}_{-1.7} \pm 1.4$	153	~ 1/4	1999, HPGe (many samples) [10]
$6.0^{+1.9}_{-1.1} \pm 0.6$	19.5	8	2001, 2xHPGe (coincidence) [11,12]
$5.7^{+1.3}_{-0.9} \pm 0.8$	37.5	3	2007, NEMO-3, (2e+2 γ) [13]
$5.5^{+1.2}_{-0.8} \pm 0.3$	35.5	8	2009, 2xHPGe (coincidence) [14]
$6.9^{+1.0}_{-0.8} \pm 0.7$	597	~ 1/10	2010, HPGe [15]
$7.5 \pm 0.6 \pm 0.6$	239	2	HPGe, 2014 [16]

Average value: $6.7^{+0.5}_{-0.4} \cdot 10^{20}$ y

References

- [9] A.S. Barabash et al., Phys. Lett. B 345 (1995) 408.
 - [10] A. S. Barabash et al., Phys. At. Nucl. 62 (1999) 2039.
 - [11] L. De Braeckeleer et al., Phys. Rev. Lett. 86 (2001) 3510.
 - [12] M.J. Hornish et al., Phys. Rev. C 74 (2006) 044314.
 - [13] R. Arnold et al., Nucl. Phys. A 781 (2007) 209.
 - [14] M.F. Kidd, et al., Nucl. Phys. A 821 (2009) 251.
 - [15] P. Belli, et al., Nucl. Phys. A 846 (2010) 143.
 - [16] R. Arnold, et al., Nucl. Phys. A 925 (2014) 25.
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Double beta decay of ^{100}Mo to the excited states [NPA 925 (2014) 25]

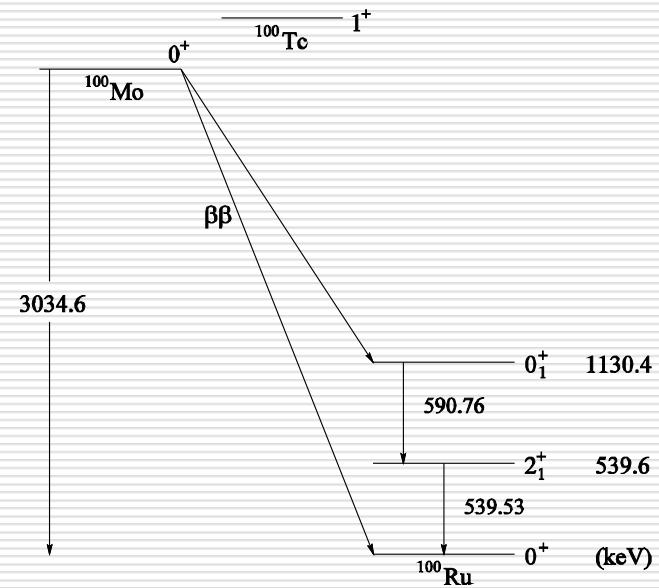
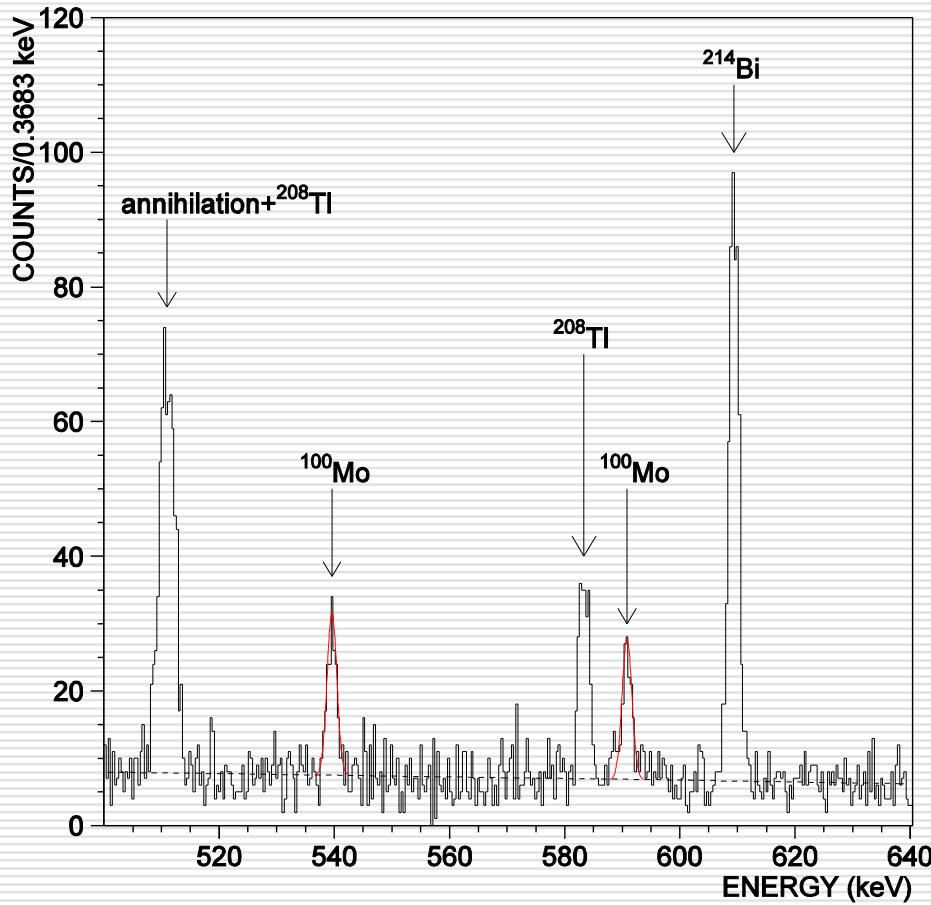
^{100}Mo source (metallic foils):

- ^{100}Mo foil was packed into bobbin, specially made for the 600 cm^3 detector (**OBELIX**)
- Mass of foils is **2588 g**
- Mass of Mo is **2583 g**
(99.8%)
- Average enrichment is **97.5%**
- Mass of ^{100}Mo is **2518 g**
(**$1.52 \cdot 10^{25}$ nuclei**)
- Measurement time is **2288 h**

**Location: LMS (Frejus, France;
4800 m w.e.)**



Double beta decay of ^{100}Mo to the excited states [NPA 925 (2014) 25]



$$E_{\gamma 1} = 539.5 \text{ keV}$$

$$E_{\gamma 2} = 590.8 \text{ keV}$$

$$T_{1/2}(2\nu) = [7.5 \pm 0.6(\text{stat}) \pm 0.6 (\text{syst})] \cdot 10^{20} \text{ yr}$$

^{150}Nd . Transition to the 0^+ excited state

I. $T_{1/2} = [1.33^{+0.36}_{-0.23}(\text{stat})^{+0.27}_{-0.13}(\text{syst})] \cdot 10^{20} \text{ yr}$

(JETP. Lett. 79 (2004) 10; PRC 79 (2009) 045501)

II. $T_{1/2} = [1.07^{+0.45}_{-0.25}(\text{stat}) \pm 0.07(\text{syst})] \cdot 10^{20} \text{ yr}$

(PRC 90 (2014) 055501)

Average value: $1.2^{+0.3}_{-0.2} \cdot 10^{20} \text{ yr}$

Comparison of NME for transition to the 0⁺ ground and 0^{+_1} excited states (for ¹⁰⁰Mo and ¹⁵⁰Nd)

- Conclusion is

$$\text{NME(g.s.)} \approx \text{NME}(0_{+1})$$

- But, in fact, it looks like:

$$\text{NME(g.s.)} \approx (1.2) \times \text{NME}(0_{+1})$$

Is this important!?

III. $2\beta(0\nu)$ -decay to excited states

Very nice signature:

2e- and **two (one)** gamma with fixed energy



Possibility to have “**zero**” background



Possibility to have high sensitivity
(if registration efficiency and energy resolution are
high enough)

3.1. $2\beta(0\nu)$ -decay to 2^+_1 excited state

Many years people thought that this decay is sensitive only to right-handed currents.

T. Tomoda demonstrated that this is not through:

“...relative sensitivity of 0^+-2^+ decays to the neutrino mass and the right-handed currents are comparable to those of 0^+-0^+ decays.”

[**T. Tomoda, Phys. Lett. B 474 (2000) 245**]

The decay is suppressed in $\sim 3\text{-}5$ order of magnitude in comparison to transition to 0^+ g.s.

Table 4. Best present limits on $2\beta(0\nu)$ -decay to 2^+_1 excited state

Nucleus	$E_{2\beta}$, keV	$T_{1/2}$, y (90% CL)
^{76}Ge	1480	$> 8.2 \cdot 10^{23}$ (G-M)
^{100}Mo	2494.5	$> 1.6 \cdot 10^{23}$ (NEMO-3)
^{130}Te	1992.7	$> 1.4 \cdot 10^{23}$ (MiBeta)
^{116}Cd	1411.5	$> 2.9 \cdot 10^{22}$ (Solotvino)
^{136}Xe	1649.4	$> 2.6 \cdot 10^{25}$ (KamLAND)
^{82}Se	2218.5	$> 1.0 \cdot 10^{22}$ (LUCIFER)

Table 5. Best present limits on $2\beta(0\nu)$ -decay to the 0_{+}^{+} excited state

Nuclus	$E_{2\beta}$, keV	$T_{1/2}$, y (90% CL)	Theory [1] ($\langle m_\nu \rangle = 1$ eV)	Theory [2] ($\langle m_\nu \rangle = 1$ eV)
^{150}Nd	2627.1	$>1.0 \cdot 10^{20}$	$1.8 \cdot 10^{25}$	-
^{96}Zr	2202.5	$>3.1 \cdot 10^{20}$	$8.8 \cdot 10^{27}$	$(0.9-1.7) \cdot 10^{24}$
^{100}Mo	1903.7	$>8.9 \cdot 10^{22}$	$2.8 \cdot 10^{25}$	$(6.4-1.2) \cdot 10^{25}$
^{82}Se	1507.5	$>3.4 \cdot 10^{22}$	$1.2 \cdot 10^{26}$	$(3.8-7.6) \cdot 10^{25}$
^{48}Ca	1274.8	$>1.5 \cdot 10^{20}$	$2.3 \cdot 10^{25}$	$7.4 \cdot 10^{25}$ [3]

Table 5 (Continue)

^{116}Cd	1056.6	$> 6.3 \cdot 10^{22}$	$(2.5\text{-}2.7) \cdot 10^{26}$	$(5.5\text{-}12) \cdot 10^{25}$
^{76}Ge	916.7	$> 6.2 \cdot 10^{21}$	$1.4 \cdot 10^{26}$	$(4.2\text{-}8.3) \cdot 10^{25}$ $2.3 \cdot 10^{26}$ [3]
^{136}Xe	878.8	$> 2.4 \cdot 10^{25}$ $(\langle m \rangle < 0.36\text{-}0.84 \text{ eV})$	$(5.8\text{-}6.4) \cdot 10^{25}$	$(3.7\text{-}7.5) \cdot 10^{24}$ $5 \cdot 10^{26}$ [3]
^{130}Te	734	$> 9.4 \cdot 10^{23}$	$(3.7\text{-}4.4) \cdot 10^{25}$	$(0.5\text{-}1.1) \cdot 10^{25}$ $6.1 \cdot 10^{27}$ [3]

[1] J. Kotila et al., PRC 85 (2012) 034316.

[2] J. Hyvarinen, J. Suhonen, PRC 93 (2016) 064306.

[3] J. Menendez et al., NPA 818 (2009) 139.

2 β (0v)-decay to 0^+_1 excited state

- Future possibilities:
 - **LEGEND** with ^{76}Ge $\rightarrow \sim 10^{27} \text{ y}$;
 - **KamLAND-Zen (1 t) with ^{136}Xe** $\rightarrow \sim 5 \cdot 10^{26} \text{ y}$;
 - **CUORE, SNO+** with ^{130}Te $\rightarrow \sim 10^{26} \text{ y}$;
 - **SuperNEMO** with ^{82}Se (or ^{150}Nd)
 $\rightarrow \sim 10^{24}-10^{25} \text{ y}$;
-

IV. ECEC to the excited states

- 1994 (A.S.B. JETP Lett. 59 (1994) 677).

Main assumption: $\text{NME}(2\nu; 0^+_{\text{g.s.}}) \approx \text{NME}(2\nu; 0^+_1)$:

then $T_{1/2}(0^+_1) \sim 10^{21}\text{-}10^{22}$ y for ^{96}Ru , ^{106}Cd , ^{124}Xe , ^{136}Ce ;

$\sim 10^{23}$ y for ^{78}Kr and ^{130}Ba

Very nice signature: in addition to **two X-rays** we have here
two gamma with strictly fixed energy ($E \sim 300\text{-}1300$ keV)



New experiments were proposed

Table 6. Best present limits on ECEC(2ν) to the 0^+_1 excited state

Nucleus, isotopical abundance	Q_{ECEC} , keV	$T_{1/2}$, y (90%CL)	Prediction
^{130}Ba ; 0.11%	829.8	$>1.5 \cdot 10^{21}$ *)	$\sim 10^{23}$
^{106}Cd ; 1.25%	1641.4	$>1 \cdot 10^{21}$	$\sim 10^{22}-10^{23}$
^{78}Kr ; 0.35%	1349.3	$>5.4 \cdot 10^{21}$	$\sim 10^{23}-10^{24}$
^{136}Ce ; 0.185%	799.5	$>1.6 \cdot 10^{18}$	$\sim 10^{23}$
^{96}Ru ; 5.54%	1566.4	$>2.5 \cdot 10^{20}$	$\sim 10^{23}-10^{24}$
^{112}Sn ; 0.97%	695.4	$>1.6 \cdot 10^{21}$	$\sim 10^{23}-10^{24}$

IV.2. ECEC(0_v); resonance conditions

Transition to the ground state. For the best candidates ($\langle m_v \rangle = 1 \text{ eV}$):

$\beta^+ \beta^+ (0v)$	$\sim 10^{28}-10^{30} \text{ y}$
$\beta^+ EC(0v)$	$\sim 10^{26}-10^{27} \text{ y}$
$ECEC(0v)$	$\sim 10^{28}-10^{31} \text{ y}$

(One can compare these values with
 $\sim 10^{24}-10^{25} \text{ y}$ for $2\beta^-$ -decay)

ECEC(0v) to the ground state



$$\begin{aligned} &+ 2\gamma \\ &+ e^+e^- \\ &+ e^-_{\text{int}} \end{aligned}$$

$$E_{\gamma,\dots} = \Delta M - \epsilon_{e1} - \epsilon_{e2}$$

Suppression factor is $\sim 10^4$ (in comparison with EC $\beta^+(0v)$) - M. Doi and T. Kotani, Prog. Theor. Phys. 89 (1993)139.

Resonance conditions

- In **1955** (**R. Winter, Phys. Rev. 100 (1955) 142**) it was mentioned that if there is excited level with “right” energy then decay rate can be very high.
($Q' - E$ has to be close to zero. Q' -energy of decay, E -energy of excited state)
 - In **1982** the same idea for transition to ground and excited states was discussed (**M. Voloshin, G. Mizelmacher, R. Eramzhan, JETP Lett. 35 (1982)**).
 - In **1983** (**J. Bernabeu, A. De Rujula, C. Jarlskog, Nucl. Phys. B 223 (1983) 15**) this idea was discussed for **^{112}Sn** (transition to 0^+ excited state). It was shown that enhancement factor can be on the level $\sim \mathbf{10^6!}$
 - In **2004** the same conclusion was done by **Z. Sujkowski and S. Wycech (Phys. Rev. C 70 (2004) 052501)**.
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Main candidates:

**^{74}Se , ^{78}Kr , ^{96}Ru , ^{102}Pd , ^{106}Cd , ^{112}Sn , ^{124}Xe , ^{130}Ba , ^{144}Sm ,
 ^{136}Ce , ^{152}Gd , ^{156}Dy , ^{162}Er , ^{164}Er , ^{168}Yb , ^{180}W , ^{184}Os , ^{190}Pt**

Resonance conditions have not been confirmed (practically for all of them). Mainly because of $\Delta Q > 1 \text{ keV}$. And, in some cases, because of **«not good» quantum numbers (spin and parity)** of the states.

**Best experimental sensitivity $\sim 10^{21} \text{ yr}$ (^{112}Sn , ^{106}Cd)
(but $\sim 10^{16}$ - 10^{19} yr in most cases)**

$^{156}\text{Dy} — ^{156}\text{Gd}$ transitions

E*, keV	I $^\pi$	e- orbitals	ΔQ , keV	EF
1946.375	1-	KL ₁	0.75(10)	$4.1 \cdot 10^6$
1952.385	0-	KM ₁	1.37(10)	$1.7 \cdot 10^6$
1988.5(2)	0⁺	L₁L₁	0.54(24)	$2.5 \cdot 10^6$
2003.749	2 ⁺	M ₁ N ₁	0.04(24)	$7.7 \cdot 10^8$

$T_{1/2} \approx 10^{28}\text{-}10^{30}$ yr (for transition to 1988.5 keV)

Problems

- There is no “good” candidate up to now
 - Concentration of isotope-candidates is low (**~ 0.1-1%**). Exception is **^{96}Ru - 5.5%**.
 - There is no «reliable» information about high energy excited states (information from 50-th and 60-th years of last century). **So, «good candidate» can be found in the future!**
-

CONCLUSION

- **2 β (2v)-decay to 0⁺ excited states was detected for ^{100}Mo and ^{150}Nd in many independent experiments.**
Next good candidates are ^{96}Zr and ^{82}Se .
 - **There are good prospects to search for 2 β (2v) and 2 β (0v)-decay to 0⁺ excited states in future large-scale experiments.**
 - **ECEC(0v) is a “new-old” possibility to search for neutrino mass (in case of resonance conditions). But still there is no «good» candidate here.**
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**J. Bernabeu, A. De Rujula, C. Jarlskog,
Nucl. Phys. B 223 (1983) 15**



$$\Delta\mathbf{M} = 1919.5 \pm 4.8 \text{ keV}$$

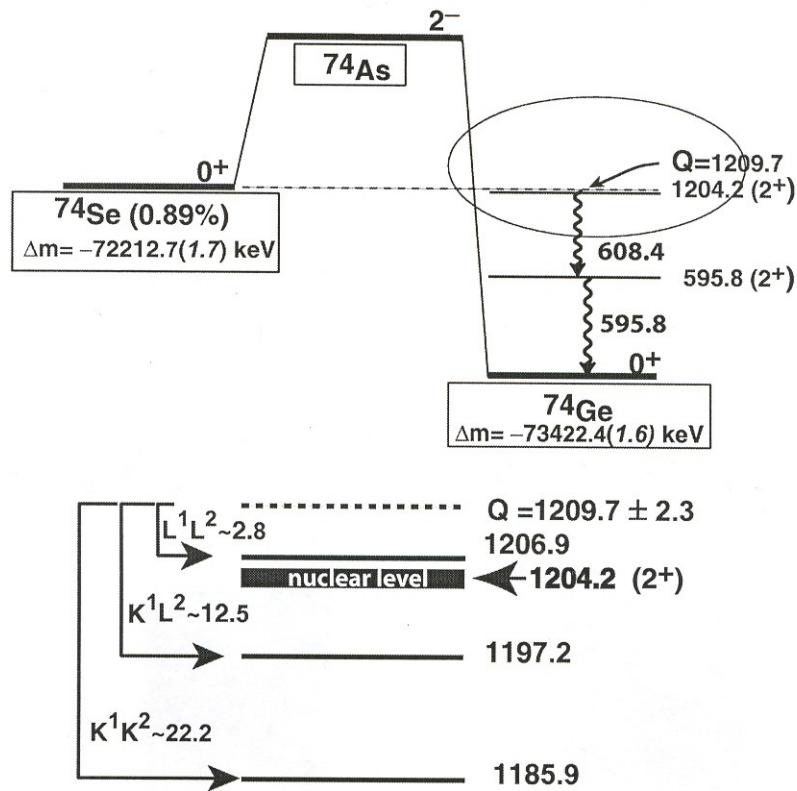
$$\begin{aligned}\Delta Q(KK;0^+) &= \Delta\mathbf{M} - E^*(0^+) - 2E_K = \\ &= (-4.9 \pm 4.8) \text{ keV}\end{aligned}$$

$T_{1/2} \approx 3 \cdot 10^{24} \text{ y (for } m_\nu = 1 \text{ eV)}$

(if $\Delta Q \sim 10 \text{ eV}$)

Present value: $\Delta Q = -4.72 \pm 0.23 \text{ keV}$

Decay-scheme of ^{74}Se



Here $Q = \Delta M = 1209.7$

$$Q' = \Delta M - 2E_b$$

$$\begin{aligned} \Delta Q'(E^*) &= Q' - 1204.2 = \\ &= 2.1 \pm 0.1 \text{ keV} \end{aligned}$$

g.s.-g.s. transitions

**^{152}Gd (0.2%), ^{164}Er (1.56%),
 ^{180}W (0.13%)**

(There are only X-rays in this case)

^{152}Gd : $\Delta Q = 0.91(18) \text{ keV} \Rightarrow$
 $T_{1/2} \approx 10^{26} \text{ y } (<\!m_\nu\!> = 1 \text{ eV})$

(Penning-trap mass spectrometry)
